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12th Public Questions (March 2020 to July 2026)

GOVT. QUESTION PAPER- MARCH 2020
12TH STANDARD – MATHEMATICS

Time Allowed : 3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.
(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. If $u(x,y) = e^{x^2+y^2}$, then $\frac{\partial u}{\partial x}$ is equal to: (1) y^2u (2) $e^{x^2+y^2}$ (3) $2xu$ (4) x^2u
2. Subtraction is not a binary operation in: (1) $\mathbb{Q}$ (2) $\mathbb{R}$ (3) $\mathbb{Z}$ (4) $\mathbb{N}$
3. The value of $\int_0^{\pi} sin^4\, x\, dx$ is: (1) $\frac{3\pi}{2}$ (2) $\frac{3\pi}{10}$ (3) $\frac{3\pi}{8}$ (4) $\frac{3\pi}{4}$
4. A polynomial equation of degree n always has:
   (1) exactly n roots (2) n distinct roots (3) n real roots (4) n imaginary roots
5. If $\rho(A) = \rho([A \setminus B])$, then the AX = B of linear equations is:
   (1) inconsistent (2) consistent and has a unique solution
   (3) consistent (4) consistent and has infinitely many solution
6. The vertex of the parabola x^2 = 8y-1 is:
   (1) $\left(0, -\frac{1}{8}\right)$ (2) $\left(-\frac{1}{8}, 0\right)$ (3) $\left(\frac{1}{8}, 0\right)$ (4) $\left(0, \frac{1}{8}\right)$
7. If $\sin^{-1} x + \sin^{-1} y = \frac{2\pi}{3}$; then $cos^{-1}x + cos^{-1}y$ is equal to: (1) π (2) $\frac{2\pi}{3}$ (3) $\frac{\pi}{3}$ (4) $\frac{\pi}{6}$
8. The value of $\sum_{i=1}^{13}(i^n + i^{n-1})$ is: (1) 0 (2) 1 + i (3) i (4) 1
9. $\vec{r}$ = s$\hat{\imath}$ + t$\hat{\jmath}$ is the equation of (s,t are parameters):
   (1) zox plane (2) a straight line joining the points $\hat{\imath}$ and $\hat{\jmath}$
   (3) xoy plane (4) yoz plane
10. The order of the differential equation of all circles with centre at (h,k) and radius ' a ' where h,k and a are arbitrary constants is : (1) 1 (2) 2 (3) 3 (4) 4
11. arg(0) is : (1) ∞ (2) 0 (3) π (4) undefined
12. $tan^{-1}\left(\frac{1}{4}\right) + \tan^{-1}\left(\frac{2}{9}\right)$ is: (1) $\tan^{-1}\left(\frac{1}{2}\right)$ (2) $\frac{1}{2}\cos^{-1}\left(\frac{3}{5}\right)$ (3) $\frac{1}{2}\sin^{-1}\left(\frac{3}{5}\right)$ (4) $\frac{1}{2}\tan^{-1}\left(\frac{3}{5}\right)$
13. The position of a particle moving along a horizontal line of any time t is given by s(t) = $3t^2$ - 2t – 8. The time at which the particle is at rest, is:
   (1) t = 3 (2) t = 0 (3) t = $\frac{1}{3}$ (4) t = 1
14. The least possible perimeter (in meter) of a rectangle of area 100 m^2 is :
   (1) 50 (2) 10 (3) 20 (4) 40
15. A random variable X has binomial distribution with $n = 25$ and $p = 0.8$, then standard deviation of X is: (1) 2 (2) 6 (3) 4 (4) 3
16. The radius of the circle $3x^2 + by^2$+ 4bx – 6by +b^2 = 0 is: (1) $\sqrt{11}$ (2) 1 (3) 3 (4) $\sqrt{10}$

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17. The distance between the planes $x + 2y + 3z + 7 = 0$ and $2x + 4y + 6z + 7 = 0$ is:

(1) $\frac{7}{2\sqrt{2}}$ (2) $\frac{\sqrt{7}}{2\sqrt{2}}$ (3) $\frac{7}{2}$ (4) $\frac{\sqrt{7}}{2}$

18. If $(AB)^{-1} = \begin{bmatrix} 12 & -17 \\ -19 & 27 \end{bmatrix}$ and $A^{-1} = \begin{bmatrix} 1 & -1 \\ -2 & 3 \end{bmatrix}$, then B^{-1} =

(1) $\begin{bmatrix} 8 & -5 \\ -3 & 2 \end{bmatrix}$ (2) $\begin{bmatrix} 2 & -5 \\ -3 & 8 \end{bmatrix}$ (3) $\begin{bmatrix} 8 & 5 \\ 3 & 2 \end{bmatrix}$ (4) $\begin{bmatrix} 3 & 1 \\ 2 & 1 \end{bmatrix}$

19. The value of $\int_0^{\frac{2}{3}} \frac{dx}{\sqrt{4-9x^2}}$ is : (1) π (2) $\frac{\pi}{6}$ (3) $\frac{\pi}{2}$ (4) $\frac{\pi}{4}$

20. The order and degree of the differential equation $\frac{dx}{dy} + \frac{dy}{dx} = 0$ are :

(1) 2, degree not defined (2) 1,2 (3) 2,1 (4) 2,2

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. Prove that $\left(\frac{1+i}{1-i}\right)^3 - \left(\frac{1-i}{1+i}\right)^3 = -2i$.

22. If (1+i)(1+2i)…….(1+ni) = x+iy, then prove that 2.5.10…….$(1+n^2) = x^2+y^2$.

23. Find the value of $sin^{-1}\left[sin\left(\frac{5\pi}{4}\right)\right]$.

24. Find the magnitude and the direction cosines of the torque about the point $(2,0,-1)$ of a force $2\hat{\imath} + \hat{\jmath} - \hat{k}$, whose line of action passes through the origin.

25. Find the value in the interval $\left(\frac{1}{2}, 2\right)$ satisfied by the Rolle's theorem for the function $f(x) = x + \frac{1}{x}, x \in \left[\frac{1}{2}, 2\right]$.

26. For the function $f(x) = x^2 + 3x$, calculate the differential df when $x = 2$ and $dx = 0.1$.

27. Prove that $\int_0^{\frac{\pi}{2}} \frac{f(sinx)}{f(sinx)+f(cosx)}$ dx = $\frac{\pi}{4}$.

28. Find the differential equation of the family of parabolas $y^2 = 4ax$, where 'a' is an arbitrary constant.

29. Prove that the identity element is unique if it exists.

30. Find the equation of the parabola if the curve is open leftward , vertex is (2,1) and passing through the point (1,3).

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. If $A = \begin{bmatrix} 2 & 9 \\ 1 & 7 \end{bmatrix}$ then prove that $(A^T)^{-1} = (A^{-1})^T$.

32. If p is real, discuss the nature of the roots of the equation $4x^2 + 4px + p + 2 = 0$, in terms of p.

33. A concrete bridge is designed as a parabolic arch. The road over bridge is $40m$ long and the maximum height of the arch is $15m$. Write the equation of the parabolic arch. Take (0,0) as the vertex.

34. Find the Vector and Cartesian equations of a straight passing through the points $(-5,7,-4)$ and $(13,-5,2)$. Find the point where the straight line crosses the xy -plane.

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35. Find the critical numbers (only x values) of the function f(x) = $x^{\frac{4}{5}}$ (x-4)^2.

36. If $U = \log(x^3 + y^3 + z^3)$ then find $\frac{\partial U}{\partial x} + \frac{\partial U}{\partial y} + \frac{\partial U}{\partial z}$.

37. A random variable *X* has the following probability mass function.

then find $P(2 < X < 6)$.

X	1	2	3	4	5	6
P(X = x)	*k*	2*k*	6*k*	5*k*	6*k*	10k

38. Let X be a continuous random variable and f(x) is defined as:

$f(x) = \begin{cases} kx(1-x)^{10}, & 0 < x < 1 \\ 0, & \text{otherwise} \end{cases}$ find the value of *k* .

39. Prove that $p \to q \equiv \neg p \vee q$.

40. If the lines $\frac{x-x_1}{l_1} = \frac{y-y_1}{m_1} = \frac{z-z_1}{n_1}$ and $\frac{x-x_2}{l_2} = \frac{y-y_2}{m_2} = \frac{z-z_2}{n_2}$ lie on the same plane, then write the number of ways to find the Cartesian equation of the above plane and explain in detail.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Test the consistency of the following system of linear equations by rank method.

$x - y + z = -9, 2x - y + z = 4, 3x - y + z = 6, 4x - y + 2z = 7$ **OR**

b) If $2\cos\alpha = x + \frac{1}{x}$ and $2\cos\beta = y + \frac{1}{y}$, show that:

(i) $\frac{x^m}{y^n} - \frac{y^n}{x^m} = 2i\sin(m\alpha - n\beta)$ (ii) $x^m y^n + \frac{1}{x^m y^n} = 2\cos(m\alpha + n\beta)$

42. a) Draw the graph of cosx in $[0,\pi]$ and $\cos^{-1}$x in [-1,1]. **OR**

b) Find the equation of the circle passing through the points (1,1),(2,-1) and (3,2).

43. a) Assume that water issuing from the end of a horizontal pipe, $7.5m$ above the ground, describes a parabolic path. The vertex of the parabolic path is at the end of the pipe. At a position $2.5m$ below the line of the pipe, the flow of water has curved outward $3m$ beyond the vertical line through the end of the pipe. How far beyond this vertical line will the water strike the ground? **OR**

b) By vector method, prove that, $\cos(\alpha + \beta) = \cos\alpha\cos\beta - \sin\alpha\sin\beta$.

44. a) Find the vector and Cartesian equation of the plane passing through the point $(0,1,-5)$ and parallel to the straight lines

$\vec{r} = (\hat{\imath} + 2\hat{\jmath} - 4\hat{k}) + s(2\hat{\imath} + 3\hat{\jmath} + 6\hat{k})$ and $\vec{r} = (\hat{\imath} - 3\hat{\jmath} + 5\hat{k}) + t(\hat{\imath} + \hat{\jmath} - \hat{k})$. **OR**

b) Evaluate $\int_{-\pi}^{\pi} \frac{\cos^2 x}{1+a^x}\,dx$

45. a) A police jeep, approaching an orthogonal intersection from the northern direction, is chasing a speeding car that has turned and moving straight east. When the jeep is 0.6 km north of the intersection and the car is 0.8 km to the east the police determine with a radar that the distance between the jeep and the car is increasing at 20 km/hr. If the jeep is moving at 60 km/hr at the instant of measurement, what is the speed of the car? **OR**

b) Find the area of the region bounded by $x-$ axis, the curve $y = |\cos x|$, the lines $x = 0$ and $x = \pi$.

46. a) A square shaped thin material with area 196 sq. units to make into an open box by cutting small equal squares from the four corners and folding the side upward. Prove that the length of the side of a removed square is $\frac{7}{3}$ when the volume of the box is maximum. **OR**

b) If F is the constant force generated by the motor of an automobile of mass M, its velocity V is given by $M\frac{dV}{dt} = F - kV$, where k is a constant. Prove that $V = \frac{F}{k}\left(1 - e^{\frac{-kt}{M}}\right)$ when $t = 0$ and V = 0.

47. a) In an investigation, a corpse was found by a detective at exactly $8\ p.m.$ Being alert, the detective also measured the body temperature and found it to be $70°F$. Two hours later, the detective measured the body temperature again and found it to be $60°F$. If the room temperature is $50°F$, and assuming that the body temperature of the person before death was $98.6°F$, prove that the time of death is 5.26 p.m. (5hrs 26 minutes) (app). $\left[\frac{\log(2.43)}{\log(2)} \simeq 1.28\right]$ **OR**

b) Three fair coins are tossed once. Find the probability mass function, mean and variance for number of heads occurred. Verify the results by binomial distribution.

GOVT. QUESTION PAPER- SEPTEMPER 2020

12TH STANDARD – MATHEMATICS

Time Allowed : 3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.
(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. If A^TA^{-1} is symmetric, then A^2 =
   (1) A^{-1} (2) $(A^T)^2$ (3) A^T (4) $(A^{-1})^2$
2. If $x^a\ y^b = e^m$, $x^c\ y^d = e^n$, $\Delta_1 = \begin{vmatrix} m & b \\ n & d \end{vmatrix}$, $\Delta_2 = \begin{vmatrix} a & m \\ c & n \end{vmatrix}$, $\Delta_3 = \begin{vmatrix} a & b \\ c & d \end{vmatrix}$, then the values of x and y are respectively:
   (1) $e^{(\Delta_2/\Delta_1)}$, $e^{(\Delta_3/\Delta_1)}$ (2) log (Δ_1 /Δ_3), log (Δ_2/ Δ_3)
   (3) log (Δ_2/Δ_1), log(Δ_3/Δ_1) (4) $e^{(\Delta_1/\Delta_3)}$, $e^{(\Delta_2/\Delta_3)}$
3. If z is a non zero complex number, such that $2iz^2 = \bar{z}$ then $|z|$ is :
   (1) $\frac{1}{2}$ (2) 1 (3) 2 (4) 3
4. If a = 3+i and z = 2-3i, then the points on the Argand diagram representing az, 3az, -az are:
   (1) Vertices of a right angled triangle (2) Vertices of an equilateral triangle
   (3) Vertices of an isosceles triangle (4) Collinear
5. The polynomial $x^3 - kx^2 + 9x$ has three real zeros if any only if, k satisfies :
   (1) $|k| \leq 6$ (2) $k = 0$ (3) $|k| > 6$ (4) $|k| \geq 6$
6. If $\cot^{-1} x = \frac{2\pi}{5}$ for some $x \in R$, the value of $\tan^{-1} x$ is:
   (1) $-\frac{\pi}{10}$ (2) $\frac{\pi}{5}$ (3) $\frac{\pi}{10}$ (4) $-\frac{\pi}{5}$

7. $sin^{-1}(cos\ x) = \frac{\pi}{2} - x$ is valid for:

(1) $-\pi \le x \le 0$ (2) $0 \le x \le \pi$ (3) $-\frac{\pi}{2} \le x \le \frac{\pi}{2}$ (4) $-\frac{\pi}{4} \le x \le \frac{3\pi}{4}$

8. The length of the latus rectum of the parabola y^2-4x+4y+8 = 0 is :

(1) 8 (2) 6 (3) 4 (4) 2

9. If the co-ordinates at one end of a diameter of the circle $x^2 + y^2 - 8x - 4y + c = 0$ are (11,2), the coordinates of the other end is : (1) $(-5,2)$ (2) $(-3,2)$ (3) $(5,-2)$ (4) $(-2,5)$

10. If $\vec{a} = \hat{\imath} + \hat{\jmath} + \hat{k}$, $\vec{b} = \hat{\imath} + \hat{\jmath}$, $\vec{c} = \hat{\imath}$ and $(\vec{a} \times \vec{b}) \times \vec{c} = \lambda\vec{a} + \mu\vec{b}$, then the value of $\lambda + \mu$ is:

(1) 0 (2) 1 (3) 6 (4) 3

11. The co-ordinates of the point where the line $\vec{r}$ = (6$\hat{\imath}$-$\hat{\jmath}$-3$\hat{k}$)+t(-$\hat{\imath}$+4$\hat{k}$) meets the plane $\vec{r}$.($\hat{\imath}$+$\hat{\jmath}$-$\hat{k}$) = 3 are: (1) (2,1,0) (2) (7,-1,-7) (3) (1,2,-6) (4) (5,-1,1)

12. Angle between $y^2 = x$ and x^2 = y at the origin is :

(1) $\tan^{-1}\frac{3}{4}$ (2) $\tan^{-1}\left(\frac{4}{3}\right)$ (3) $\frac{\pi}{2}$ (4) $\frac{\pi}{4}$

13. The number given by the Rolle's theorem for the function x^3 - $3x^2$, $x \in$ [0,3] is :

(1) 1 (2) $\sqrt{2}$ (3) $\frac{3}{2}$ (4) 2

14. If $W(x, y) = x^y$, $x > 0$, then $\frac{\partial W}{\partial x}$ is equal to :

(1) $x^y \log x$ (2) y log x (3) yx^{y-1} (4) x log y

15. The value of $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \left(\frac{sinx}{2+cosx}\right) dx$ is : (1) 0 (2) 2 (3) log 2 (4) log 4

16. If f $(x) = \int_0^x t \cot t\ dt$, then $\frac{df}{dx}$ =

(1) cos x – x sin x (2) sin x+ x cos x (3) x cos x (4) x sin x

17. If cosx is an integrating factor of the differential equation $\frac{dy}{dx} + Py = Q$, then P =

(1) -cotx (2) cotx (3) tan x (4) -tanx

18. The solution of the differential equation $\frac{dy}{dx} = \frac{y}{x} + \frac{\emptyset\left(\frac{y}{x}\right)}{\emptyset'\left(\frac{y}{x}\right)}$ is :

(1) $x\emptyset\left(\frac{y}{x}\right)$ = k (2) $\emptyset\left(\frac{y}{x}\right)$ = kx (3) y$\emptyset\left(\frac{y}{x}\right)$ = k (4) $\emptyset\left(\frac{y}{x}\right)$ = ky

19. In 16 throws of a die getting an even number is considered a success, then the variance of the successes is: (1) 4 (2) 6 (3) 2 (4) 256

20. The operation $*$ defined by $a * b = \frac{ab}{7}$ is not a binary operation on:

(1) $\mathbb{Q}^+$ (2) $\mathbb{Z}$ (3) $\mathbb{R}$ (4) $\mathbb{C}$

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. Find the least positive integer n such that $\left(\frac{1+i}{1-i}\right)^n$ = 1.

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22. Obtain the Cartesian equation for the locus of $z = x + iy$ in $|z + i| = |z - 1|$.
23. If α, β, γ and δ are the roots of the polynomial equation $2x^4 + 5x^3 - 7x^2 + 8 = 0$, find a quadratic equation with integer coefficients whose roots are $\alpha + \beta + \gamma + \delta$ and $\alpha\beta\gamma\delta$.
24. Find the principal value of $\tan^{-1}(\sqrt{3})$.
25. If $\hat{a}, \hat{b}, \hat{c}$ are three unit vectors such that $\hat{b}$ and $\hat{c}$ are non-parallel and $\hat{a} \times (\hat{b} \times \hat{c}) = \frac{1}{2}\hat{b}$, find the angle between $\hat{a}$ and $\hat{c}$.
26. Evaluate the limit: $\lim_{x \to 0} \left(\frac{\sin mx}{x}\right)$
27. Evaluate $\int_3^4 \frac{dx}{x^2 - 4}$
28. Find the differential equation of the family of y = ax^2+bx+c where a,b are parameters and c is a constant.
29. Examine the binary operation of the operation a$*$b = $\left(\frac{a-1}{b-1}\right)$, $\forall$ a,b $\in$ Q.
30. Show that, if x = r$\cos\theta$, y = r$\sin\theta$, then $\frac{\partial r}{\partial x}$ is equal to $\cos\theta$.

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Verify $(AB)^{-1} = B^{-1}A^{-1}$ with $A = \begin{bmatrix} 0 & -3 \\ 1 & 4 \end{bmatrix}, B = \begin{bmatrix} -2 & -3 \\ 0 & -1 \end{bmatrix}$
32. If $A = \begin{bmatrix} 8 & -4 \\ -5 & 3 \end{bmatrix}$, verify that $A(adj\ A) = (adj\ A)A = |A|I$.
33. Obtain the condition that the roots of $x^3 + px^2 + qx + r = 0$ are in A.P.
34. A circle of area 9π square units has two of its diameters along the lines $x + y = 5$ and $x - y = 1$. Find the equation of the circle.
35. Prove that with usual notations $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$ by using area of the triangle property.
36. Find the absolute extrema of the function $f(x) = x^2 - 12x + 10$ on [1,2] .
37. Suppose that z = ye^{x^2}, where $x = 2t$ and y = 1-t then find $\frac{dz}{dt}$.
38. Two fair coins are tossed simultaneously. Find the probability mass function for number of heads occurred.
39. The mean and variance of a binomial variate X are respectively 2 and 1.5. Find $P(X = 0)$.
40. Show that ((~q)$\wedge$p))$\wedge$q is a contradiction.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Test for consistency and if possible, solve the following systems of equations by rank method.
$2x + 2y + z = 5, x - y + z = 1, 3x + y + 2z = 4$ **OR**
b) Prove that arg(z_1z_2) = arg(z_1) + arg(z_2)
42. a) Draw the graph of tanx in $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ and $\tan^{-1}$x in $(-\infty, \infty)$. **OR**
b) Find the centre, foci and eccentricity of the hyperbola: $11x^2 - 25y^2 - 44x + 50y - 256 = 0$.

43. a) A rod of length $1.2m$ moves with its ends always touching the coordinate axes. The locus of a point P on the rod, which is $0.3m$ from the end in contact with x -axis is an ellipse. Find the eccentricity. **OR**

b) Using vector method, prove that $\cos(\alpha - \beta) = \cos\alpha\cos\beta + \sin\alpha\sin\beta$.

44. a) Find the Vector and Cartesian equation of the plane passing through the point $(1, -2, 4)$ and perpendicular to the plane $x + 2y - 3z = 11$ and parallel to the line $\frac{x+7}{3} = \frac{y+3}{-1} = \frac{z}{1}$. **OR**

b) Prove that among all the rectangles of the given perimeter, the square has the maximum area.

45. a) Show that $\int_0^1 (\tan^{-1} x + \tan^{-1}(1-x))dx = \frac{\pi}{2} - log\ 2$. **OR**

b) A pot of boiling water at $100°C$ is removed from a stove at time t = 0 and left to cool in the kitchen. After 5 minutes, the water temperature has decreased to $80°C$, and another 5 minutes later it has dropped to $65°C$. Determine the temperature of the kitchen.

46. a) Solve $\frac{dy}{dx} = e^{x+y} + x^3e^y$ **OR**

b) If $X \sim B(n, p)$ such that $4P(X = 4) = P(X = 2)$ and $n = 6$, find the distribution, mean and standard deviation of X.

47. a) A Car A is travelling from west at 50 km/hr and Car B is travelling towards north at 60 km/hr. Both are headed for the intersection of the two roads. At what rate are the Cars approaching each other when Car A is 0.3 kilometers and Car B is 0.4 kilometers from the intersection? **OR**

b) Find the area of region bounded by the ellipse $\frac{x^2}{25} + \frac{y^2}{16} = 1$ and its latus rectums.

GOVT. QUESTION PAPER- AUGUST 2021

12TH STANDARD – MATHEMATICS

PART – I 20x1 = 20

Note: (i) Answer all the questions.
(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. The inverse of $\begin{bmatrix} 3 & 1 \\ 5 & 2 \end{bmatrix}$ is :

(1) $\begin{bmatrix} 3 & -1 \\ -5 & -3 \end{bmatrix}$ (2) $\begin{bmatrix} 2 & -1 \\ -5 & 3 \end{bmatrix}$ (3) $\begin{bmatrix} -3 & 5 \\ 1 & -2 \end{bmatrix}$ (4) $\begin{bmatrix} -2 & 5 \\ 1 & -3 \end{bmatrix}$

2. The centre of the hyperbola $\frac{(x-1)^2}{16} - \frac{(y+1)^2}{25} = 1$ is :

(1) $\left(\frac{1}{2}, -\frac{1}{2}\right)$ (2) (-1,1) (3) (1,-1) (4) (0,0)

3. The order and degree of the differential equation $\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^{1/3} + x^{1/4} = 0$ are:

(1) 2,6 (2) 2,3 (3) 2,4 (4) 3,3

4. A pair of dice numbered 1, 2, 3, 4, 5, 6 of a six sided die and 1, 2, 3, 4 of a four sided die is rolled and the sum is determined. If the random variable X denote this sum then the number of elements in the inverse image of 7 is : (1) 3 (2) 1 (3) 4 (4) 2

5. If $|z|$ = 1, then the value of $\frac{1+z}{1+\bar{z}}$ is : (1) $\frac{1}{z}$ (2) z (3) 1 (4) $\bar{z}$

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6. The value of $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} sin^2 x \cos x \, dx$ is : (1) 0 (2) $\frac{3}{2}$ (3) $\frac{2}{3}$ (4) $\frac{1}{2}$

7. The function $f(x) = x^2$, in the interval $[0,\infty)$ is :
   (1) cannot be determined (2) increasing function
   (3) increasing and decreasing function (4) decreasing function

8. The volume of the parallelepiped with its edges represented by the vectors $\hat{\imath} + \hat{\jmath}, \hat{\imath} + 2\hat{\jmath}, \hat{\imath} + \hat{\jmath} + \pi\hat{k}$ is: (1) π (2) $\frac{\pi}{2}$ (3) $\frac{\pi}{4}$ (4) $\frac{\pi}{3}$

9. In the set $\mathbb{R}$ of real numbers '*' is defined as follows. Which one of following is **not** a binary operation on $\mathbb{R}$? (1) a*b = a (2) a * b = min (a,b) (3) a * b = a^b (4) a * b = max (a,b)

10. The position of a particle 's' moving at any time t is given by s(t) = $5t^2$ - 2t – 8. The time at which the particle is at rest, is : (1) 1 (2) 0 (3) 5 (4) $\frac{1}{5}$

11. If the function $f(x) = \frac{1}{12}$ for $a < x < b$, represents a probability density function of a continuous random variable X, then which of the following cannot be the value of a and b ?
   (1) 7 and 19 (2) 0 and 12 (3) 16 and 24 (4) 5 and 17

12. If P (x, y) be any point on $16x^2 + 25y^2 = 400$ with foci $F_1(3, 0)$ and F_2 (-3, 0) then $PF_1 + PF_2$ is :
   (1)10 (2) 8 (3)12 (4) 6

13. If the planes $\vec{r}.(2\hat{\imath} - \lambda\hat{\jmath} + \hat{k}) = 3$ and $\vec{r}.(4\hat{\imath} + \hat{\jmath} - \mu\hat{k}) = 5$ are parallel, then the value of λ and μ are respectively :
   (1) $-\frac{1}{2}$, -2 (2) $\frac{1}{2}$, -2 (3) $\frac{1}{2}$, 2 (4) $-\frac{1}{2}$, 2

14. A zero of $x^3 + 64$ is : (1) 4i (2) 0 (3) -4 (4) 4

15. The solution of $\frac{dy}{dx} + P(x)y = 0$ is :
   (1) $x = ce^{-\int Pdy}$ (2) $y = ce^{\int Pdx}$ (3) $x = ce^{\int Pdy}$ (4) $y = ce^{-\int Pdx}$

16. $\int_0^{\frac{\pi}{2}} \sin^7 x \, dx =$ (1) $\frac{\pi}{2}$ (2) $\int_0^{\frac{\pi}{2}} \cos^7 x \, dx$ (3) 0 (4) 1

17. The value of $\sin^{-1}\left(\frac{1}{2}\right) + \cos^{-1}\left(\frac{1}{2}\right)$ is: (1) 0 (2) $\frac{\pi}{2}$ (3) $\frac{\pi}{3}$ (4) π

18. If A,B and C are invertible matrices of some order, then which one of the following is **not true**?
   (1) det $A^{-1} = (detA)^{-1}$ (2) adjA = $|A|\ A^{-1}$
   (3) $(ABC)^{-1} = C^{-1}B^{-1}A^{-1}$ (4) adj(AB) = (adjA)(adjB)

19. The value of the complex number $(i^{25})^3$ is equal to : (1) 1 (2) i (3) –i (4) -1

20. If we measure the side of a cube to be 4cm with an error of 0.1cm, then the error in calculation of the volume is (in cube cm) : (1) 2 (2) 0.4 (3) 4.8 (4) 0.45

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. If $z = (2 + 3i)(1 - i)$ then prove that $z^{-1} = \frac{5}{26} - i\frac{1}{26}$.

22. If α and β are the roots of x^2-5x+6 = 0 then prove that $\alpha^2 - \beta^2 = \pm 5$.

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23. For what value of x does $\sin x = \sin^{-1} x$?

24. Show that the three vectors $2\hat{\imath} + 3\hat{\jmath} + \hat{k}, \hat{\imath} - 2\hat{\jmath} + 2\hat{k}$ and $3\hat{\imath} + \hat{\jmath} + 3\hat{k}$ are coplanar.

25. Prove that $\lim_{x\to\infty}\left(\frac{e^x}{x^m}\right)$, where m is a positive integer, is ∞.

26. If $g(x) = x^2 + \sin x$, then find dg.

27. Show that the solution of $\frac{dy}{dx} = \sqrt{\frac{1-y^2}{1-x^2}}$ is $\sin^{-1}y = \sin^{-1}x + C$ or $\sin^{-1}x = \sin^{-1}y + C$.

28. If X is the random variable with distribution function $F(x)$, given by:

$F(x) = \begin{cases} 0 & ; -\infty < x < 0 \\ \frac{1}{2}(x^2 + x) & ; 0 \le x < 1 \\ 1 & ; 1 \le x < \infty \end{cases}$ then prove that the p.d.f is $f(x) = \begin{cases} \frac{1}{2}(2x+1); & 0 \le x < 1 \\ 0 & ; \text{ otherwise} \end{cases}$

29. The probability density function of X is given by $f(x) = \begin{cases} kxe^{-2x}, & x > 0 \\ 0, & x \le 0 \end{cases}$. Prove that the value of k is 4.

30. Show that the differential equation corresponding to y = Asinx, where A is an arbitrary constant, is $y = y'\tan x$.

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Show that the rank of the matrix $\begin{bmatrix} 0 & 1 & 2 & 1 \\ 0 & 2 & 4 & 3 \\ 8 & 1 & 0 & 2 \end{bmatrix}$ is 3.

32. If $A = \begin{bmatrix} 8 & -4 \\ -5 & 3 \end{bmatrix}$, verify that $A(adj\ A) = (adj\ A)A = |A|I$.

33. Show that the points $1, \frac{-1}{2} + i\frac{\sqrt{3}}{2}$ and $\frac{-1}{2} - i\frac{\sqrt{3}}{2}$ are the vertices of an equilateral triangle of side length $\sqrt{3}$.

34. If the sides of a cubic box are increased by 1, 2, 3 units respectively to form a cuboid, then the volume is increased by 52 cubic units. Show that the volume of the cuboid is 60 cubic units.

35. Prove that the equation of the parabola with focus (4,0) and directrix $x = -4$ is $y^2 = 16x$.

36. A force $13\hat{\imath} + 10\hat{\jmath} - 3\hat{k}$ acts on a particle which is displaced from the point with position vector $4\hat{\imath} - 3\hat{\jmath} - 2\hat{k}$ to the point with position vector $6\hat{\imath} + \hat{\jmath} - 3\hat{k}$. Show that the work done by the force is 69 units.

37. Show that the point on the curve $y = x^2 - 5x + 4$ at which the tangent is parallel to the line $3x + y = 7$, is (1,0).

38. An egg of a particular bird is spherical in shape. If the radius to the inside of the shell is 4 mm and radius to the outside of the shell is 4.2 mm, prove that the approximate volume of the shell is 12.8π mm^3.

39. Define an operation $*$ on $\boldsymbol{Q}$ as follows: $a * b = \left(\frac{a+b}{2}\right); a, b \in \boldsymbol{Q}$. Examine the closure and commutative properties satisfied by $*$ on $\mathbb{Q}$.

40. Show that $\int_0^1 \frac{\sqrt{x}}{\sqrt{1-x}+\sqrt{x}}dx = \frac{1}{2}$

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PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Solve the system of equations $x - y + 2z = 2, 2x + y + 4z = 7, 4x - y + z = 4$ by Cramer's rule. **OR**

b) A camera is accidentally knocked off an edge of a cliff $400\ ft.$ high. The camera falls a distance of $s = -16t^2$ in t seconds. Show that the camera hits the ground when t = 5 seconds and also prove that the velocity when it hits the ground is -160 ft./sec.

42. a) If $z = x + iy$ is a complex number such that $\left|\frac{z-4i}{z+4i}\right| = 1$, show that the locus of z is real axis or y = 0. **OR**

b) Show that $\int_0^1 \sqrt{\frac{1-x}{1+x}}\,dx = \frac{\pi}{2} - 1$.

43. a) Prove that $\cos^{-1}\left[\cos\left(\frac{4\pi}{3}\right)\right] + \cos^{-1}\left[\cos\left(\frac{5\pi}{4}\right)\right] = \frac{17\pi}{12}$. **OR**

b) Find the eccentricity, centre , vertices and foci of the ellipse $\frac{x^2}{16} + \frac{y^2}{9} = 1$ and also draw the rough diagram.

44. a) Solve $(e^y + 1)\cos x\,dx + e^y \sin x\,dy = 0$ **OR**

b) Show that $\neg(p \to q) \equiv p \wedge (\neg q)$.

45. a) Using Vector method, prove that $\cos(A - B) = \cos A \cos B + \sin A \sin B$. **OR**

b) Find two positive numbers whose product is 20 and their sum is minimum.

46. a) On lighting a rocket cracker it gets projected in a parabolic path and reaches a maximum height of $4m$ when it is $6m$ away from the point of projection. Finally it reaches the ground $12m$ away from the starting point. Show that the angle of projection is $\tan^{-1}\left(\frac{4}{3}\right)$. **OR**

b) A random variable X has the following probability mass function:

x	1	2	3	4	5
$f(x)$	k^2	$2k^2$	$3k^2$	$2k$	$3k$

Find: (i) the value of k (ii) $P(2 \le X < 5)$ (iii) $P(3 < X)$.

47. a) Show that the area of the region bounded by $3x - 2y + 6 = 0, x = -3\ and\ x = 1$ is $\frac{15}{2}$. **OR**

b) Show that the Cartesian equation of the plane passing through the points (1,2,3) and (2,3,1) and also perpendicular to the plane $3x - 2y + 4z + 5 = 0$ is $2y + z - 7 = 0$.

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GOVT. QUESTION PAPER- MAY 2022

12TH STANDARD – MATHEMATICS

Time Allowed : 3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.
(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. If $f(x) = \begin{cases} 2x & 0 \le x \le a \\ 0 & \text{otherwise} \end{cases}$ is a probability density function of a random variable, then the value of a is: (a) 3 (b) 1 (c) 4 (d) 2
2. Which one of the following is not true in the case of discrete random variable X?
   (a) $\lim_{x\to\infty} F(x)$ = F(∞) = 1 (b) 0 ≤ F(x) ≤ 1 for all x∈ **R**
   (c) F(x) is real valued decreasing function (d) $\lim_{x\to-\infty} F(x)$ = F(−∞) = 0
3. If f(x) = $\frac{x}{x+1}$,then its differential is:
   (a) $\frac{1}{x+1}dx$ (b) $\frac{-1}{(x+1)^2}dx$ (c) $\frac{-1}{x+1}dx$ (d) $\frac{1}{(x+1)^2}dx$
4. The value of $\int_0^1 x(1-x)^{99}\,dx$ is :
   (a) $\frac{1}{10010}$ (b) $\frac{1}{11000}$ (c) $\frac{1}{10001}$ (d) $\frac{1}{10100}$
5. The principal value of $\cos^{-1}\left(\frac{\sqrt{3}}{2}\right)$ is: (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{3}$ (c) $\frac{5\pi}{6}$ (d) $\frac{\pi}{6}$
6. If A = $\begin{bmatrix} 2 & 3 \\ 5 & -2 \end{bmatrix}$ be such that λA^{-1} = A, then λ is: (a)19 (b) 17 (c) 21 (d) 14
7. If α,β and γ are the zeros of $x^3 + px^2 + qx + r$, then $\sum\frac{1}{\alpha}$ is:
   (a) $\frac{q}{r}$ (b) $-\frac{q}{r}$ (c) $-\frac{q}{p}$ (d) $-\frac{p}{r}$
8. If (1+i)(1+2i)(1+3i)…….(1+ni) = x+iy then the value 2.5.10…….(1+n^2) is:
   (a) x^2+y^2 (b) 1 (c) $1 + n^2$ (d) i
9. The minimum value of the function $|3-x|$+9 is: (a) 6 (b) 0 (c) 9 (d) 3
10. The value of $\sum_{n=1}^{12} i^n$ is: (a) 0 (b) 1 (c) -1 (d) i
11. If the vectors $2\hat{\imath} - \hat{\jmath} + 3\hat{k}$, $3\hat{\imath} + 2\hat{\jmath} + \hat{k}$ and $\hat{\imath} + m\hat{\jmath} + 4\hat{k}$ are coplanar, then the value of m is: (a) 2 (b) 3 (c) -2 (d) -3
12. The general equation of a circle with centre (-3,-4) and radius 3 units is:
   (a) $x^2 + y^2 - 6x + 8y - 16 = 0$ (b) $x^2 + y^2 - 6x - 8y + 16 = 0$
   (c) $x^2 + y^2 + 6x - 8y + 16 = 0$ (d) $x^2 + y^2 + 6x + 8y + 16 = 0$

13. The solution of $\frac{dy}{dx} + p(x)y = 0$ is:

(a) $x = ce^{-\int pdy}$ (b) $y = ce^{\int pdx}$ (c) $x = ce^{\int pdy}$ (d) $y = ce^{-\int pdx}$

14. The value of $\int_0^\infty e^{-3x}x^2\,dx$ is: (a) $\frac{4}{27}$ (b) $\frac{7}{27}$ (c) $\frac{2}{27}$ (d) $\frac{5}{27}$

15. The point of inflection of the curve y = $(x-1)^3$ is:

(a) (1,0) (b) (0,0) (c) (1,1) (d) (0,1)

16. The angle between the lines $\frac{x-4}{2} = \frac{y}{1} = \frac{z+1}{-2}$ and $\frac{x-1}{4} = \frac{y+1}{-4} = \frac{z-2}{2}$ is:

(a) $\frac{\pi}{2}$ (b) $\frac{\pi}{4}$ (c) $\frac{2\pi}{3}$ (d) $\frac{\pi}{3}$

17. Which one of the following is a binary operation on ℕ?

(a) Multiplication (b) Division (c) Subtraction (d)All the above

18. Which of the following is **incorrect**?

(a) If A is a square matrix of order n, and λ is a scalar, then Adj(λA) = λ^nAdj(A).

(b) Adjoint of a symmetric matrix is also a symmetric matrix.

(c) A(adjA) = (adjA)A = $|A|$I.

(d) Adjoint of a diagonal matrix is also a diagonal matrix.

19. If $\sin x$ is the integrating factor of the linear differential equation $\frac{dy}{dx} + Py = Q$, then P is:

(a) $\tan x$ (b) $\log \sin x$ (c) $\cot x$ (d) $\cos x$

20. The length of the latus rectum of the parabola x^2=24y is: (a) 8 (b) 24 (c) 6 (d) 12

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. Prove the following properties: $Re(z) = \frac{z+\bar{z}}{2}$ and $Im(z) = \frac{z-\bar{z}}{2i}$

22. Find a polynomial equation of minimum degree with rational coefficients, having $2-\sqrt{3}$ as a root.

23. Find the principal value of $\tan^{-1}(\sqrt{3})$.

24. Find the points on the curve $y = x^3 - 3x^2 + x - 2$ at which the tangent is parallel to the line $y = x$.

25. Find df for $f(x) = x^2 + 3x$ and evaluate it for $x = 2$ and $dx = 0.1$.

26. Show that the differential equation of the family of curves y = $Ae^x + Be^{-x}$, where A and B are arbitrary constants, is $\frac{d^2y}{dx^2}$ - y = 0.

27. Solve: $\frac{dy}{dx} = \sqrt{\frac{1-y^2}{1-x^2}}$

28. A random variable *X* has the following probability mass function.

Find k.

x	1	2	3	4	5	6
f (x)	*k*	2*k*	6*k*	5*k*	6*k*	10k

29. X is the number of tails occurred when three fair coins are tossed simultaneously. Find the values of the random variable X and number of points in its inverse images.
30. Show that the distance from the origin to the plane 3x+6y+2z+7 = 0 is 1.

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Show that the rank of the matrix $\begin{bmatrix} 1 & 2 & -1 \\ 3 & -1 & 2 \\ 1 & -2 & 3 \\ 1 & -1 & 1 \end{bmatrix}$ is 3.
32. Solve the following system of linear equations, using matrix inversion method:
$5x + 2y = 3,\ 3x + 2y = 5$.
33. Which one of the points $10 - 8i$, $11 + 6i$ is closest to $1 + i$.
34. Solve the equation $2x^3 - 9x^2 + 10x = 3$, if 1 is a root, find the other root.
35. Find the magnitude and the direction cosines of the torque about the point $(2,0,-1)$ of a force $2\hat{\imath} + \hat{\jmath} - \hat{k}$, whose line of action passes through the origin.
36. Evaluate: $\lim_{x\to\infty} \frac{2x^2-3}{x^2-5x+3}$
37. Assume that the cross section of the artery of human is circular. A drug is given to a patient to dilate his arteries. If the radius of an artery is increased from 2 mm to 2.1 mm, how much is cross-sectional area increased approximately.
38. Show that $\int_0^{\frac{\pi}{3}} \frac{\sec x \tan x}{1+\sec^2 x}\, dx = \tan^{-1}(2) - \frac{\pi}{4}$.
39. Let $*$ be defined on **R** by $(a * b) = a + b + ab - 7$. Is $*$ binary on **R** ? If so, find $3 * \left(\frac{-7}{15}\right)$.
40. Prove that the general equation of the circle whose diameter is the line segment joining the points (-4,-2) and (-1,-1), is $x^2 + y^2 + 5x + 3y + 6 = 0$.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Cramer's rule is not applicable to solve the system 3x+y+z = 2, x-3y+2z = 1, 7x-y+4z = 5. Why?

OR

b) Prove that the local minimum values for the function $f(x) = 4x^6 - 6x^4$ attain at -1 and 1.

42. a) Show that the locus of $z = x + iy$ if $|z + i| = |z - 1|$, is $x + y = 0$. **OR**

b) Show that $\int_0^a \frac{f(x)}{f(x)+f(a-x)}\, dx = \frac{a}{2}$.

43. a) Show that the equation of the parabola with focus $(-\sqrt{2}, 0)$ and directrix $x = \sqrt{2}$ is $y^2 = -4\sqrt{2}x$

OR

b) Find the value of $\cot^{-1}(1) + \sin^{-1}\left(-\frac{\sqrt{3}}{2}\right) - \sec^{-1}(-\sqrt{2})$.

44. a) The maximum and minimum distances of the Earth from the Sun respectively are $152 \times 10^6 km$ and $94.5 \times 10^6 km$. The Sun is at one focus of the elliptical orbit. Show that the distance from the Sun to the other focus is 575×10^5 km. **OR**

b) Prove by vector method that $\sin(A+B) = \sin A \,.\cos B + \cos A.\sin B$.

45. a) Find the vector equation(any form) or Cartesian equations of the plane passing through the points (2,2,1), (9,3,6) and perpendicular to the plane $2x + 6y + 6z = 9$. **OR**

b) Show that the angle between the curves $y = x^2$ and $x = y^2$ at (1,1) is $tan^{-1}\left(\frac{3}{4}\right)$.

46. a) The distribution function of a continuous random variable X is:

$$F(x) = \begin{cases} 0, & x < 1 \\ \frac{x-1}{4}, & 1 \le x \le 5 \\ 1, & x > 5 \end{cases}$$

Find (i) $P(X < 3)$ (ii) $P(2 < X < 4)$ (iii) $P(3 \le X)$ **OR**

b) Show that the area of the region bounded by $3x - 2y + 6 = 0$, $x = -3, x = 1$ and x-axis, is $\frac{15}{2}$.

47. a) Show that the solution of the differential equation $(1 + x^2)\frac{dy}{dx} = 1 + y^2$ is $tan^{-1}y = tan^{-1}x$ + C (or) $tan^{-1}x = tan^{-1}y$ + C **OR**

b) Prove $p \to (q \to r) \equiv (p \wedge q) \to r$ using truth table.

GOVT. QUESTION PAPER- JULY 2022

12TH STANDARD – MATHEMATICS

Time Allowed : 3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.

(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. If $A = \begin{bmatrix} \frac{3}{5} & \frac{4}{5} \\ x & \frac{2}{5} \end{bmatrix}$ and $A^T = A^{-1}$, then the value of x is :
   (a) $\frac{-4}{5}$ (b) $\frac{-3}{5}$ (c) $\frac{3}{5}$ (d) $\frac{4}{5}$
2. If A is a non-singular matrix such that $A^{-1} = \begin{bmatrix} 5 & 3 \\ -2 & -1 \end{bmatrix}$ then $(A^T)^{-1}$ =
   (a) $\begin{bmatrix} -5 & 3 \\ 2 & 1 \end{bmatrix}$ (b) $\begin{bmatrix} 5 & 3 \\ -2 & -1 \end{bmatrix}$ (c) $\begin{bmatrix} -1 & -3 \\ 2 & 5 \end{bmatrix}$ (d) $\begin{bmatrix} 5 & -2 \\ 3 & -1 \end{bmatrix}$
3. If z = x+iy is a complex number such that $|z + 2| = |z - 2|$, then the locus of z is : (a) real axis (b) imaginary axis (c) ellipse (d) circle
4. $i^n + i^{n+1} + i^{n+2} + i^{n+3}$ is : (a) 0 (b) 1 (c) -1 (d) i
5. A zero of $x^3 + 64$ is : (a) 0 (b) 4 (c) 4i (d) – 4
6. The principal value of $\cos^{-1}\left(cos\frac{\pi}{6}\right)$ is: (a) $\frac{\pi}{6}$ (b) $\frac{5\pi}{6}$ (c) $\frac{-\pi}{6}$ (d) $\frac{\pi}{3}$
7. The equation of the circle passing through the foci of the ellipse $\frac{x^2}{16} + \frac{y^2}{9} = 1$ having centre at (0,3) is :
   (a) $x^2 + y^2 - 6y - 7 = 0$ (b) $x^2 + y^2 - 6y + 7 = 0$

(c) $x^2 + y^2 - 6y - 5 = 0$ (d) $x^2 + y^2 - 6y + 5 = 0$

8. The eccentricity of the hyperbola $\frac{x^2}{16} - \frac{(y-3)^2}{4} = 1$ is :

(a) $\frac{\sqrt{3}}{2}$ (b) $\frac{\sqrt{5}}{2}$ (c) $\sqrt{5}$ (d) $\frac{1}{2}$

9. If a vector $\vec{\alpha}$ lies in the plane of $\vec{\beta}$and $\vec{\gamma}$ then :

(a) $[\vec{\alpha},\vec{\beta},\vec{\gamma}\,] = 1$ (b) $[\vec{\alpha},\vec{\beta},\vec{\gamma}\,] = -1$ (c) $[\vec{\alpha},\vec{\beta},\vec{\gamma}\,] = 0$ (d) $[\vec{\alpha},\vec{\beta},\vec{\gamma}\,] = 2$

10. Distance from the origin to the plane $3x - 6y + 2z + 7 = 0$ is :

(a) 0 (b) 1 (c) 2 (d) 3

11. A stone is thrown up vertically. The height it reaches at time t seconds is given by $x = 80t - 16t^2$. The stone reaches the maximum height in time t seconds is given by :

(a) 2 (b) 2.5 (c) 3 (d) 3.5

12. The angle between the parabolas $y^2 = x$ and $x^2 = y$ at the origin is :

(a) $\frac{\pi}{4}$ (b) $\frac{\pi}{6}$ (c) $\frac{\pi}{2}$ (d) 0

13. The percentage error of fifth root of 31 is approximately how many times the percentage error in 31? (a) $\frac{1}{31}$ (b) $\frac{1}{5}$ (c) 5 (d) 31

14. The value of $\int_{-1}^{2} |x|\, dx$ is: (a) $\frac{1}{2}$ (b) $\frac{3}{2}$ (c) $\frac{5}{2}$ (d) $\frac{7}{2}$

15. The area between $y^2 = 4x$ and its latus rectum is :

(a) $\frac{2}{3}$ (b) $\frac{4}{3}$ (c) $\frac{8}{3}$ (d) $\frac{5}{3}$

16. The order of the differential equation of all circles with centre at (h, k) and radius ' a ' is _____

(where h,k are arbitrary constants) (a) 2 (b) 3 (c) 4 (d) 1

17. The differential equation representing the family of curves y = A cos (x+ B) ,

where A and B are parameters , is :

(a) $\frac{d^2y}{dx^2}$ - y = 0 (b) $\frac{d^2y}{dx^2}$ + y = 0 (c) $\frac{d^2y}{dx^2} = 0$ (d) $\frac{d^2x}{dy^2} = 0$

18. If a fair die is thrown once then the probability to get a prime number on the face is :

(a) 0 (b) $\frac{1}{2}$ (c) $\frac{1}{4}$ (d) $\frac{1}{6}$

19. A random variable X takes the probability mass function:

X	-2	3	1
P(X=x)	$\frac{\lambda}{6}$	$\frac{\lambda}{4}$	$\frac{\lambda}{12}$

The value of λ is : (a) 1 (b) 2 (c) 3 (d) 4

20. Which one of the following is a binary operation on $\mathbb{N}$?

(a) Subtraction (b) Multiplication (c) Division (d) All the above

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PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. Find df for $f(x) = x^2 + 3x$ and evaluate it for $x = 3$ and dx $= 0.02$.
22. If α and β are the roots of x^2+5x+6 = 0 , then show that $\alpha^2 + \beta^2 = 13$.
23. Find the value of $\sin^{-1}(1) + \cos^{-1}(1)$.
24. Find the acute angle between the two straight lines $\frac{x-4}{2} = \frac{y}{1} = \frac{z+1}{-2}$ and $\frac{x-1}{4} = \frac{y+1}{-4} = \frac{z-2}{2}$.
25. Find the tangent to the curve $y = x^2 - x^4$ at (1,0).
26. If $z_1 = 3, z_2 = -7i$ and $z_3 = 5 + 4i$, show that $z_1(z_2 + z_3) = z_1z_2 + z_1z_3$.
27. Show that y = $ae^x + be^{-x}$ is a solution of the differential equation y''-y = 0.
28. A random variable X has the following probability mass function.

x	1	2	3	4	5
$f(x)$	k^2	$2k^2$	$3k^2$	$2k$	$3k$

Show that the value of k is $\frac{1}{6}$.

29. Suppose the amount of milk sold daily at a milk booth is distributed with a minimum of 200 litres and a maximum of 600 litres with probability density function X is:
$f(x) = \begin{cases} k, & 200 \le x \le 600 \\ 0, & \text{otherwise} \end{cases}$. Find the value of *k*.
30. Form the differential equation of the curve y = ax^2+bx+c where a,b and c are arbitrary constant.

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Verify $(AB)^{-1} = B^{-1}A^{-1}$ with $A = \begin{bmatrix} 0 & -3 \\ 1 & 4 \end{bmatrix}, B = \begin{bmatrix} -2 & -3 \\ 0 & -1 \end{bmatrix}$
32. Find the rank of the matrix $\begin{bmatrix} 1 & -2 & 3 \\ 2 & 4 & -6 \\ 5 & 1 & -1 \end{bmatrix}$
33. Show that the square root of $6 - 8i$ are $\pm(2\sqrt{2}\text{-i}\sqrt{2})$.
34. Prove that the roots of the equation x^4 - 3x^2- 4 = 0 are $\pm$2, $\pm$i.
35. Find centre and radius of the circles $x^2 + y^2 + 6x - 4y + 4 = 0$
36. A particle acted on by constant forces $8\hat{\imath} + 2\hat{\jmath} - 6\hat{k}$ and $6\hat{\imath} + 2\hat{\jmath} - 2\hat{k}$ is displaced from the point (1,2,3) to the point (5, 4,1) . Find the total work done by the forces.
37. Show that $\lim_{x \to 0^+} x \log x$ is 0.
38. A circular plate expands uniformly under the influence of heat. If its radius increases from 10.5 cm to 10.75cm, then find an approximate change in the area
39. Verify (i) closure property (ii) commutative property of the following operation on the given set. $(a * b) = a^b; \forall\, a, b \in N$ (exponentiation property)
40. Prove that $\int_0^1 xe^x dx$ = 1

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PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Solve the system of linear equation by Cramer's Rule

$3x + 3y - z = 11, 2x - y + 2z = 9, 4x + 3y + 2z = 25$ **OR**

b) A particle is fired straight up from the ground to reach a height of *s* feet in *t* seconds, where $s(t) = 128t - 16t^2$. (i) Compute the maximum height of the particle reached. (ii) What is the velocity when the particle hits the ground?

42. a) Show that $\left(2 + i\sqrt{3}\right)^{10} - \left(2 - i\sqrt{3}\right)^{10}$ is purely imaginary. **OR**

b) Find the area of the region bounded by the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ using integration.

43. a) Show that the value of $\sin^{-1}\left(\sin\frac{5\pi}{9}\cos\frac{\pi}{9} + \cos\frac{5\pi}{9}\sin\frac{\pi}{9}\right)$ is $\frac{\pi}{3}$. **OR**

b) The parabolic communication antenna has a focus at $2mts$. distance from the vertex of the antenna. Show that the width of the antenna $3mts$. from the vertex is $4\sqrt{6}$ mts.

44. a) Solve the differential equation $\frac{dy}{dx} + \frac{y}{x} = \sin x$. **OR**

b) Verify whether the following compound propositions are tautologies or contradictions or contingency. $(p \to q) \leftrightarrow (\neg p \to q)$

45. a) Prove by using vector method, prove that $\cos(A - B) = \cos A \cos B + \sin A \sin B$. **OR**

b) Prove that among all the rectangles of the given perimeter, the square has the maximum area.

46. a) Find the eccentricity, foci, vertices, and centre for the ellipse $\frac{x^2}{25} + \frac{y^2}{9} = 1$ and draw the rough diagram. **OR**

b) The cumulative distribution function of a discrete random variable is given by:

$$F(x) = \begin{cases} 0 & -\infty < x < 0 \\ \frac{1}{2} & 0 \le x < 1 \\ \frac{3}{5} & 1 \le x < 2 \\ \frac{4}{5} & 2 \le x < 3 \\ \frac{9}{10} & 3 \le x < 4 \\ 1 & 4 \le x < \infty \end{cases}$$

Find (i) the probability mass function (ii) P(X < 3) and (iii) $P(X \ge 2)$

47. a) Show that the area between the parabola y^2 = 16x and its latus rectum (using integration) is $\frac{128}{3}$. **OR**

b) Show that the Cartesian equation of the plane passing through the points $(a, 0, 0)$, $(0, b, 0)$, $(0, 0, c)$ is $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$.

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GOVT. QUESTION PAPER- MARCH 2023

12TH STANDARD – MATHEMATICS

Time Allowed : 3.00 Hours **Max.Marks : 90**

PART – I 20x1 = 20

Note: (i) Answer all the questions.

(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. A square matrix A of order n has inverse if and only if:
   (a) $\rho(A) > n$ (b) $\rho(A) = n$ (c) $\rho(A) \neq n$ (d) $\rho(A) < n$
2. Distance from the origin to the plane $3x - 6y + 2z + 7 = 0$ is:
   (a) 2 (b) 0 (c) 3 (d) 1
3. If $3\cos^{-1}x = \cos^{-1}(4x^3 - 3x)$, (a) $x \in \left(\frac{1}{2}, 1\right)$ (b) $x \in \left[\frac{1}{2}, 1\right]$ (c) $x \in (-\infty, 1]$ (d) $x \in [\frac{1}{2}, \infty)$
4. The general solution of the differential equation $\frac{dy}{dx} = \frac{y}{x}$ is:
   (a) $y = kx$ (b) $xy = k$ (c) $\log y = kx$ (d) $y = k\log x$
5. The number of normal that can be drawn from a point to the parabola $y^2 = 4ax$ is:
   (a) 3 (b) 2 (c) 0 (d) 1
6. If $\vec{a}$ and $\vec{b}$ are parallel vectors then $[\vec{a}, \vec{c}, \vec{b}]$ is equal to: (a) 1 (b) 2 (c) 0 (d) -1
7. The number of real numbers in $[0, 2\pi]$ satisfying $\sin^4 x - 2\sin^2 x + 1$ is:
   (a) 1 (b) 2 (c) ∞ (d) 4
8. Suppose that X takes on one of the values 0, 1 and 2. If for some constant k, $P(X = i) = kP(X = i - 1)$ for i =1, 2 and $P(X = 0) = \frac{1}{7}$, then the value of k is:
   (a) 3 (b) 1 (c) 4 (d) 2
9. The maximum value of the function x^2e^{-2x} , x > 0 is:
   (a) $\frac{1}{e^2}$ (b) $\frac{1}{e}$ (c) $\frac{4}{e^4}$ (d) $\frac{1}{2e}$
10. The operation $*$ defined by $a * b = \frac{ab}{7}$ is not a binary operation on:
    (a) $\mathbb{R}$ (b) $\mathbb{Q}^+$ (c) $\mathbb{C}$ (d) $\mathbb{Z}$
11. The area between $y^2 = 4x$ and its latus rectum is: (a) $\frac{8}{3}$ (b) $\frac{2}{3}$ (c) $\frac{5}{3}$ (d) $\frac{4}{3}$
12. Angle between the curves $y^2 = x$ and $x^2 = y$ at the origin is:
    (a) $\frac{\pi}{2}$ (b) $\tan^{-1}\left(\frac{3}{4}\right)$ (c) $\frac{\pi}{4}$ (d) $\tan^{-1}\left(\frac{4}{3}\right)$
13. $|adj(adjA)| = |A|^{16}$, then the order of the matrix A is: (a) 2 (b) 3 (c) 5 (d) 4
14. The value of $\left(\frac{1+i}{\sqrt{2}}\right)^8 + \left(\frac{1-i}{\sqrt{2}}\right)^8$ is: (a) 8 (b) 4 (c) 2 (d) 6
15. If $|z| = 1$, then the value of $\frac{1+z}{1+\bar{z}}$ is:

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(a) $\frac{1}{z}$ (b) z (c) 1 (d) $\bar{z}$

16. The abscissa of the point on the curve f (x) = $\sqrt{8-2x}$ at which the slope of the tangent is – 0.25? (a) - 2 (b) – 8 (c) 0 (d) -4

17. The value of $\int_0^{\frac{\pi}{3}} tanx dx$ is : (a) –log 2 (b) log 2 (c) –log 3 (d) log 3

18. The number of positive zeros of the polynomial $\sum_{r=0}^{n} nC_r(-1)^r x^r$ is:
(a) < n (b) 0 (c) r (d) n

19. The Principle value of $\sin^{-1}\left(\frac{-1}{2}\right)$ is: (a) $\frac{-\pi}{6}$ (b) 0 (c) $\frac{-\pi}{2}$ (d) $\frac{\pi}{2}$

20. Area of the greatest rectangle inscribed in the ellipse $\frac{x^2}{a^2}+\frac{y^2}{b^2}=1$ is:
(a) $\sqrt{ab}$ (b) 2ab (c) $\frac{a}{b}$ (d) ab

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. If $|z| = 2$, show that $3 \leq |z+3+4i| \leq 7$

22. If p and q are the roots of the equation $lx^2+nx+n=0$, show that $\sqrt{\frac{p}{q}}+\sqrt{\frac{q}{p}}+\sqrt{\frac{n}{l}}=0$.

23. If $y=4x+c$ is a tangent to the circle $x^2+y^2=9$, find c.

24. If the radius of a sphere with radius 10 cm, has to decrease by $0.1cm$, approximately how much will its volume decrease?

25. Evaluate: $\int_b^{\infty} \frac{1}{a^2+x^2}\,dx$, $a>0, b\in\mathbb{R}$

26. Find the vector equation of a plane which is at a distance of 7 units from the origin having $3,-4,5$ as direction ratios of a normal to it.

27. Let $A=\begin{bmatrix}0 & 1\\ 1 & 1\end{bmatrix}$,$B=\begin{bmatrix}1 & 1\\ 0 & 1\end{bmatrix}$ be any two Boolean matrices of the same type. Find $A \vee B$ and $A \wedge B$.

28. Prove that $\begin{bmatrix}\cos\theta & -\sin\theta\\ \sin\theta & \cos\theta\end{bmatrix}$ is orthogonal.

29. Find the equations of tangent to the curve $y=x^2+3x-2$ at the point $(1,2)$.

30. Express $e^{cos\theta+isin\theta}$ in a+ib form.

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Find the equation of the parabola with vertex (-1,-2), axis parallel to y -axis and passing through (3,6).

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32. The maximum and minimum distances of the Earth from the Sun respectively are $152 \times 10^6 km$ and $94.5 \times 10^6 km$. The Sun is at one focus of the elliptical orbit. Find the distance from the Sun to the other focus.
33. For what value of x, the inequality $\frac{\pi}{2} < \cos^{-1}(3x-1) < \pi$ holds?
34. Find the angle made by the straight line $\frac{x+3}{2} = \frac{y-1}{2} = -z$ with coordinate axes.
35. Use the linear approximation to find approximate values of $(123)^{\frac{2}{3}}$.
36. Solve : $x \cos y \, dy = e^x (x \log x + 1) dx$
37. If $F(\alpha) = \begin{bmatrix} \cos\alpha & 0 & \sin\alpha \\ 0 & 1 & 0 \\ -\sin\alpha & 0 & \cos\alpha \end{bmatrix}$, show that $[F(\alpha)]^{-1} = F(-\alpha)$.
38. Show that $p \to q$ and $q \to p$ are not equivalent.
39. If $z = (2+3i)(1-i)$, then find z^{-1}.
40. If a+b+c = 0 and a,b,c are rational numbers then, prove that the roots of the equation (b+c-a)x^2+(c+a-b)x+(a+b-c) = 0 are rational numbers.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Solve the equation $z^3 + 8i = 0$, where $z \in \mathbb{C}$ **OR**

b) Solve: $(1 + x + xy^2)\frac{dy}{dx} + (y + y^3) = 0$.

42. a) Using vector method, prove that $\cos(\alpha - \beta) = \cos\alpha \cos\beta + \sin\alpha \sin\beta$. **OR**

b) Suppose the amount of milk sold daily at a milk booth is distributed with a minimum of 200 litres and a maximum of 600 litres with probability density function of random variable X is $f(x) = \begin{cases} k & 200 \le x \le 600 \\ 0 & \text{otherwise} \end{cases}$. Find (i) the value of k (ii) the distribution function (iii) the probability that daily sales will fall between 300 litres and 500 litres.

43. a) Identify the type of conic and find centre, foci and vertices of

$18x^2 + 12y^2 - 144x + 48y + 120 = 0$. **OR**

b) If $\cos^{-1} x + \cos^{-1} y + \cos^{-1} z = \pi$ and $0 < x, y, z < 1$, show that

$x^2 + y^2 + z^2 + 2xyz = 1$

44. a) A boy is walking along the path $y = ax^2 + bx + c$ through the points$(-6,8), (-2,-12)$ and $(3,8)$. He wants to meet his friend at P$(7,60)$. Will he meet his friend? (Use Gaussian Elimination method) **OR**

b) Prove that the ellipse $x^2 + 4y^2 = 8$ and the hyperbola $x^2 - 2y^2 = 4$ intersect orthogonally.

45. a) Find the parametric form of Vector equation and Cartesian equations of the plane containing the line $\vec{r} = (\hat{\imath} - \hat{\jmath} + 3\hat{k}) + t(2\hat{\imath} - \hat{\jmath} + 4\hat{k})$ and perpendicular to the plane $\vec{r}.(\hat{\imath} + 2\hat{\jmath} + \hat{k}) = 8$.

OR

b) Solve the equation $6x^4 - 5x^3 - 38x^2 - 5x + 6 = 0$ if it is known that $\frac{1}{3}$ is a solution.

46. a) Prove that $p \to (\neg q \vee r) \equiv \neg p \vee (\neg q \vee r)$ using truth table.

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b) Suppose a person deposits Rs.10,000 in a bank account at the rate of 5% per annum compounded continuously. How much money will be in his bank account 18 months later?

47. a) Find the maximum value of $\frac{logx}{x}$. **OR**

b) Find the smaller area of the region common to the ellipse $\frac{x^2}{a^2}+\frac{y^2}{b^2}=1$ and the line $\frac{x}{a}+\frac{y}{b}=1$.

GOVT. QUESTION PAPER- JUNE 2023

12TH STANDARD – MATHEMATICS

Time Allowed :3.00 Hours **Max.Marks : 90**

PART – I

1. If A^TA^{-1} is symmetric, then A^2 is:
   a) A^{-1} b) $(A^T)^2$ c) A^T d) $(A^{-1})^2$
2. The rank of the matrix $\begin{bmatrix}1&2&3&4\\2&4&6&8\\-1&-2&-3&-4\end{bmatrix}$ is:
   a) 1 b) 2 c) 4 d) 3
3. If $|z-2+i|\le 2$, then the greatest value of $|z|$ is:
   a) $\sqrt{3}$-2 b) $\sqrt{3}$+2 c) $\sqrt{5}$-2 d) $\sqrt{5}$+2
4. If $|z_1|=1, |z_2|=2, |z_3|=3$ and $|9z_1z_2+4z_1z_3+z_2z_3|=12$ then the value of $|z_1+z_2+z_3|$ is: a) 1 b) 2 c) 3 d) 4
5. A zero of x^3+64 is: a) 0 b) 4 c) 4i d) – 4
6. The number of positive zeros of the polynomial $\sum_{r=0}^{n} nC_r(-1)^r x^r$ is:
   a) 0 b) n c) < n d) r
7. If $\cot^{-1}x=\frac{2\pi}{5}$ for some $x\in R$, then value of $\tan^{-1}x$ is:
   a) $-\frac{\pi}{10}$ b) $\frac{\pi}{5}$ c) $\frac{\pi}{10}$ d) $\frac{-\pi}{5}$
8. The radius of the circle $3x^2+by^2+4bx-6by+b^2=0$ is:
   a) 1 b) 3 c) $\sqrt{10}$ d) $\sqrt{11}$
9. If $\vec{a}.\vec{b}=\vec{b}.\vec{c}=\vec{c}.\vec{a}=0$ then the value of $[\vec{a},\vec{b},\vec{c}]$ is:
   a) $|\vec{a}||\vec{b}||\vec{c}|$ b) $\frac{1}{3}|\vec{a}||\vec{b}||\vec{c}|$ c) 1 d) -1
10. If $\sin^{-1}x+\cot^{-1}\left(\frac{1}{2}\right)=\frac{\pi}{2}$ then the value of x is:
    a) $\frac{1}{2}$ b) $\frac{1}{\sqrt{5}}$ c) $\frac{2}{\sqrt{5}}$ d) $\frac{\sqrt{3}}{2}$
11. The number given by the mean value theorem for the function $\frac{1}{x}$, $x\in[1, 9]$ is:
    a) 2 b) 2.5 c) 3 d) 3.5
12. The curve $y=ax^4+bx^2$ with a,b > 0
    a) has on horizontal tangent b) is concave up
    c) is concave down d) has no points of inflection
13. If $u(x,y)=e^{x^2+y^2}$ then $\frac{\partial u}{\partial x}$ is: a) $e^{x^2+y^2}$ b) $2xu$ c) x^2u d) y^2u

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14. The value of $\int_{-1}^{2}|x|\,dx$ is: a) $\frac{1}{2}$ b) $\frac{3}{2}$ c) $\frac{5}{2}$ d) $\frac{7}{2}$

15. Linear approximation for g (x) = cos x at $x = \frac{\pi}{2}$ is:

a) $x + \frac{\pi}{2}$ b) $- x + \frac{\pi}{2}$ c) $x - \frac{\pi}{2}$ d) $-x - \frac{\pi}{2}$

16. The value $\int_0^{\pi} sin^4\, x\, dx$ is:

a) $\frac{3\pi}{10}$ b) $\frac{3\pi}{8}$ c) $\frac{3\pi}{4}$ d) $\frac{3\pi}{2}$

17. The solution of the differential equation $\frac{dy}{dx} = 2xy$ is:

a) $y = Ce^{x^2}$ b) $y = 2x^2 + C$ c) $y = Ce^{-x^2}$ d) $y = x^2 + C$

18. The population P in any year t is such that the rate of increase in the populations is proportional to the population then:

a) P = Ce^{kt} b) P = Ce^{-kt} c) P = Ckt d) P = C

19. A random variable X- has binomial distribution with $n = 25$ and $p = 0.8$ then standard deviation of X is: a) 6 b) 4 c) 3 d) 2

20. If a compound statement involves 3 simple statements, then the number of rows in the truth table is: a) 9 b) 8 c) 6 d) 3

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. If $adj(A) = \begin{bmatrix} 0 & -2 & 0 \\ 6 & 2 & -6 \\ -3 & 0 & 6 \end{bmatrix}$ then find A^{-1}.

22. Find the principal argument $Arg z$, when $z = \frac{-2}{1+i\sqrt{3}}$.

23. Find the equation of the hyperbola with vertices $(0, \pm 4)$ and foci $(0, \pm 6)$.

24. Find the distance of a point $(2,5,-3)$ to the plane $\vec{r}.\left(6\hat{\imath} - 3\hat{\jmath} + 2\hat{k}\right) = 5$.

25. Prove that the function $f(x) = x^2 - 2x - 3$ is strictly increasing in $(2, \infty)$.

26. Show that the percentage error in the n^{th} root of a number is approximately $\frac{1}{n}$ times the percentage error in the number.

27. Evaluate : $\int_0^{\infty} x^5 e^{-3x} dx$

28. Assume that a spherical rain drop evaporates at a rate proportional to its surface area. Form a differential equation involving the rate of change of the radius of the rain drop

29. A pair of fair dice is rolled once. Find the probability mass function to get the number of fours.

30. Let $A = \begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix}$, $B = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$ be any two Boolean matrices of the same type. Find $A \vee B$ and $A \wedge B$.

PART-III

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Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Solve the system of linear equations $2x + 5y = -2,\ x + 2y = -3$ using matrix inversion method.
32. State and prove triangle inequality.
33. Find the value of $\sin^{-1}\left(\sin\frac{5\pi}{9}\cos\frac{\pi}{9} + \cos\frac{5\pi}{9}\sin\frac{\pi}{9}\right)$
34. With usual notations in any triangle *ABC*, prove by vector method that $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$
35. Find two positive numbers whose sum is 12 and their product is maximum.
36. If $U(x, y, z) = \log(x^3 + y^3 + z^3)$, find $\frac{\partial U}{\partial x} + \frac{\partial U}{\partial y} + \frac{\partial U}{\partial z}$.
37. Prove that the point of intersection of the tangents at ' t_1 ' and 't_2 'on the parabola $y^2 = 4ax$ is $[at_1t_2, a(t_1 + t_2)]$.
38. Find the population of a city at any time *t*, given that the rate of increase of population is proportional to the population at that instant and that in a period of 40 years the population increased from 3,00,000 to 4,00,000.
39. Establish the equivalence property connecting the bi-conditional with conditional:
$p \leftrightarrow q \equiv (p \to q) \wedge (q \to p)$
40. Show that the polynomial $9x^9 + 2x^5 - x^4 - 7x^2 + 2 = 0$ has at least six imaginary roots.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Solve the system of linear equations by Cramer's Rule.
$x_1 - x_2 = 3,\ 2x_1 + 3x_2 + 4x_3 = 17,\ x_2 + 2x_3 = 7$ **OR**

b) Solve $\tan^{-1}\left(\frac{x-1}{x-2}\right) + \tan^{-1}\left(\frac{x+1}{x+2}\right) = \frac{\pi}{4}$

42. a) If $z = x + iy$ and $\arg\left(\frac{z-i}{z+2}\right) = \frac{\pi}{4}$, show that $x^2 + y^2 + 3x - 3y + 2 = 0$. **OR**

b) If $u = \sin^{-1}\left(\frac{x+y}{\sqrt{x}+\sqrt{y}}\right)$, prove that $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = \frac{1}{2}\tan u$.

43. a) Evaluate: $\lim_{x\to\frac{\pi}{2}} (\sin x)^{\tan x}$ **OR**

b) If $\vec{a} = 2\hat{\imath} + 3\hat{\jmath} - \hat{k}, \vec{b} = 3\hat{\imath} + 5\hat{\jmath} + 2\hat{k}, \vec{c} = -\hat{\imath} - 2\hat{\jmath} + 3\hat{k}$, verify that $\left(\vec{a} \times \vec{b}\right) \times \vec{c} = (\vec{a}.\vec{c})\vec{b} - (\vec{b}.\vec{c})\vec{a}$

44. a) Solve the equation $2x^3 + 11x^2 - 9x - 18 = 0$. **OR**

b) Solve: $(1 + x^2)\frac{dy}{dx} = 1 + y^2$.

45. a) Find the equation of the circle through the points (1,0), (-1,0) , and (0,1). **OR**

b) The mean and variance of a binomial variate *X* are respectively 2 and 1.5 respectively. Find
(i) $P(X = 0)$ (ii) $P(X = 1)$ (iii) $P(X \geq 1)$

46. a) Find the foot of the perpendicular drawn from the point (5, 4, 2) to the line $\frac{x+1}{2} = \frac{y-3}{3} = \frac{z-1}{-1}$. Also, find the equation of the perpendicular. **OR**

b) Find the area of the region bounded by the lines $5x - 2y = 15$,$x + y + 4 = 0$ and the *x*-axis

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using integration.

47. a) A particle moves along a line according to the law $s(t) = 2t^3 - 9t^2 + 12t - 4$, where t ≥ 0 .

(i) At what times the particle changes direction?

(ii) Find the total distance travelled by the particle in the first 4 seconds.

(iii) Find the particle's acceleration each time the velocity is zero. **OR**

b) Let $M = \left\{\begin{pmatrix} x & x \\ x & x \end{pmatrix} : x \in R - \{0\}\right\}$ and let $*$ be the matrix multiplication. Examine the closure, associative, existence of identity, existence of inverse for the operation $*$ on M .

GOVT. QUESTION PAPER- MARCH 2024

12TH STANDARD – MATHEMATICS

Time Allowed :3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.

(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. The angle between the line $\vec{r} = (\hat{\imath} + 2\hat{\jmath} - 3\hat{k}) + t(2\hat{\imath} + \hat{\jmath} - 2\hat{k})$ and the plane $\vec{r} \cdot (\hat{\imath} + \hat{\jmath}) + 4 = 0$ is: (a) 45° (b) 0° (c) 90° (d) 30°
2. The number of rows in the truth table of $(p \vee q) \wedge (p \vee r)$ is: (a) 6 (b) 9 (c) 3 (d) 8
3. The area between y^2 = 4x and its latus rectum is: (a) $\frac{8}{3}$ (b) $\frac{2}{3}$ (c) $\frac{5}{3}$ (d) $\frac{4}{3}$
4. If P (x, y) be any point on $16x^2 + 25y^2 = 400$ with foci $F_1(3, 0)$ and F_2 (-3, 0) then $PF_1 + PF_2$ is: (a) 10 (b) 8 (c) 12 (d) 6
5. If $\sin^{-1} x + \cot^{-1}\left(\frac{1}{2}\right) = \frac{\pi}{2}$, then x is equal to: (a) $\frac{2}{\sqrt{5}}$ (b) $\frac{1}{2}$ (c) $\frac{\sqrt{3}}{2}$ (d) $\frac{1}{\sqrt{5}}$
6. A zero of $x^3 + 64$ is: (a) 4i (b) 0 (c) - 4 (d) 4
7. If α, β and γ are the zeros of $x^3 + px^2 + qx + r$ then $\sum \frac{1}{\alpha}$ is: (a) $\frac{q}{r}$ (b) $-\frac{q}{r}$ (c) $-\frac{q}{p}$ (d) $-\frac{p}{r}$
8. The value of $\int_0^a \left(\sqrt{a^2 - x^2}\right)^3 dx$ is: (a) $\frac{3\pi a^2}{8}$ (b) $\frac{\pi a^3}{16}$ (c) $\frac{3\pi a^4}{8}$ (d) $\frac{3\pi a^4}{16}$
9. If A, B and C are invertible matrices of some order, then which one of the following is not true?

(a) det $A^{-1} = (detA)^{-1}$ (b) adjA = $|A|$ A^{-1}

(c) $(ABC)^{-1} = C^{-1}B^{-1}A^{-1}$ (d) adj(AB) = (adjA)(adjB)

10. If a vector $\vec{\alpha}$ lies in the plane of $\vec{\beta}$ and $\vec{\gamma}$, then:
(a) $[\vec{\alpha}, \vec{\beta}, \vec{\gamma}\ ] = 0$ (b) $[\vec{\alpha}, \vec{\beta}, \vec{\gamma}\ ] = 1$ (c) $[\vec{\alpha}, \vec{\beta}, \vec{\gamma}\ ] = 2$ (d) $[\vec{\alpha}, \vec{\beta}, \vec{\gamma}\ ] = -1$
11. The differential equation of the family of curves $y = Ae^x + Be^{-x}$, where A and B are arbitrary constants is:

(a) $\frac{dy}{dx} + y = 0$ (b) $\frac{d^2y}{dx^2} + y = 0$ (c) $\frac{dy}{dx} - y = 0$ (d) $\frac{d^2y}{dx^2} - y = 0$

12. A random variable X has binomial distribution with $n = 25$ and $p = 0.8$ then standard deviation of X is: (a) 3 (b) 6 (c) 2 (d) 4

13. The type of conic section for x^2-3 = 5x + 3y is:
(a) hyperbola (b) ellipse (c) circle (d) parabola

14. If $|z_1| = 1, |z_2| = 2, |z_3| = 3$ and $|9z_1z_2 + 4z_1z_3 + z_2z_3| = 12$ then the value of $|z_1 + z_2 + z_3|$ is: (a) 1 (b) 2 (c) 3 (d) 4

15. If A is a non-singular matrix such that $A^{-1} = \begin{bmatrix} 5 & 3 \\ -2 & -1 \end{bmatrix}$, then $(A^T)^{-1}$=

(a) $\begin{bmatrix} -1 & -3 \\ 2 & 5 \end{bmatrix}$ (b) $\begin{bmatrix} -5 & 3 \\ 2 & 1 \end{bmatrix}$ (c) $\begin{bmatrix} 5 & -2 \\ 3 & -1 \end{bmatrix}$ (d) $\begin{bmatrix} 5 & 3 \\ -2 & -1 \end{bmatrix}$

16. If (1+i)(1+2i)(1+3i)…….(1+ni) = x+iy then2.5.10…….(1+n^2) is:

(a) x^2+y^2 (b) 1 (c) $1 + n^2$ (d) i

17. The horizontal asymptote of f(x) = $\frac{1}{x}$ is : (a) x = c (b) y = 0 (c) y = c (d) x = 0

18. The value of Var(3) is : (a) 0 (b) 3 (c) Var(3) (d) 9

19. The number given by the Rolle's theorem for the function x^3 - $3x^2$, $x \in$ [0,3] is:
(a) $\frac{3}{2}$ (b) 1 (c) 2 (d) $\sqrt{2}$

20. If f(x) = $\frac{x}{x+1}$,then its differential is given by:
(a) $\frac{-1}{(x+1)^2}$ dx (b) $\frac{1}{(x+1)^2}$ dx (c) $\frac{1}{x+1}$ dx (d) $\frac{-1}{x+1}$ dx

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. Simplify: $\sum_{n=1}^{12} i^n$

22. If α and β are the roots of the quadratic equation $2x^2 - 7x + 13 = 0$, construct a quadratic equation whose roots are α^2 and β^2 .

23. Find df for $f(x) = x^2 + 3x$ and evaluate it for $x = 3$ and $dx = 0.02$.

24. Find the differential equation for the family of all straight lines passing through the origin.

25. For the random variable X with the given probability mass function .

$f(x) = \begin{cases} 2(x-1) & 1 < x < 2 \\ 0 & otherwise \end{cases}$ Find the Mean.

26. Find the general equation of a circle with centre (-3,-4) and radius 3 units.

27. Find the rank of the matrix $\begin{bmatrix} -1 & 3 \\ 4 & -7 \\ 3 & -4 \end{bmatrix}$.

28. Evaluate: $\int_0^{\frac{\pi}{2}} \sin^{10} x \, dx$

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29. Evaluate: $\lim_{x\to 1} \frac{x^2-3x+2}{x^2-4x+3}$

30. Show that the vectors $2\hat{\imath} - \hat{\jmath} + 3\hat{k}$, $\hat{\imath} - \hat{\jmath}$ and $3\hat{\imath} - \hat{\jmath} + 6\hat{k}$ are coplanar.

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Show that $\cot^{-1}\left(\frac{1}{\sqrt{x^2-1}}\right) = \sec^{-1} x\,, |x| > 1.$

32. Find the equations of tangent and normal to the parabola $x^2 + 6x + 4x + 5 = 0$ at $(1, -3)$.

33. Prove that $\left[\vec{a} - \vec{b}, \vec{b} - \vec{c}, \vec{c} - \vec{a}\right] = 0.$

34. If $u(x, y) = \frac{x^2+y^2}{\sqrt{x+y}}$, prove that $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = \frac{3}{2}u$.

35. Find two positive numbers whose sum is 12 and their product is maximum.

36. Evaluate: $\int_{\frac{\pi}{8}}^{\frac{3\pi}{8}} \frac{1}{1+\sqrt{\tan x}}\,dx$

37. Simplify $\left(\frac{1+i}{1-i}\right)^3 - \left(\frac{1-i}{1+i}\right)^3$ into rectangular form.

38. Solve: $(1 + x^2)\frac{dy}{dx} = 1 + y^2.$

39. Three fair coins are tossed simultaneously. Find the probability mass function for number of heads occurred.

40. If A = $\begin{bmatrix} 2 & -1 & 3 \\ -5 & 3 & 1 \\ -3 & 2 & 3 \end{bmatrix}$, then find $|adj(adjA)|$.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Find the angle between the curves $y = x^2$ and $y = (x-3)^2$. **OR**

b) Solve: $\tan^{-1}\left(\frac{x-1}{x-2}\right) + \tan^{-1}\left(\frac{x+1}{x+2}\right) = \frac{\pi}{4}$

42. a) A six sided die is marked '1' on one face, '3' on two of its faces, and '5' on remaining three faces. The die is thrown twice. If *X* denotes the total score in two throws, find: (i) the probability mass function (ii) the cumulative distribution function (iii) $P(4 \le X < 10)$ **OR**

b) If $z = x + iy$ is a complex number such that $\text{Im}\left(\frac{2z+1}{iz+1}\right) = 0$, show that the locus of *z* is $2x^2 + 2y^2 + x - 2y = 0.$

43. a) A conical water tank with vertex down of 12 meters height has a radius of 5 meters at the top. If water flows into the tank at a rate 10 cubic m/min, how fast is the depth of the water increases when the water is 8 meters deep? **OR**

b) Prove by vector method that $\sin(\alpha - \beta) = \sin\alpha\cos\beta - \cos\alpha\sin\beta.$

44. a) Assume that water issuing from the end of a horizontal pipe, $7.5m$ above the ground, describes a parabolic path. The vertex of the parabolic path is at the end of the pipe. At a position $2.5m$ below the line of the pipe, the flow of water has curved outward $3m$ beyond the vertical line

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through the end of the pipe. How far beyond this vertical line will the water strike the ground?

OR

b) Solve the Linear differential equation $\frac{dy}{dx}+\frac{y}{x}=\sin x$.

45. a) The rate of increase in the number of bacteria in a certain bacteria culture is proportional to the number present. Given that the number triples in 5 hours, find how many bacteria will be present after 10 hours? **OR**

b) Find the vector and Cartesian equation of the plane containing $\frac{x-2}{2}=\frac{y-2}{3}=\frac{z-1}{3}$ and parallel to the $\frac{x+1}{3}=\frac{y-1}{2}=\frac{z+1}{1}$.

46. a) Find the area of the region bounded by the ellipse $\frac{x^2}{a^2}+\frac{y^2}{b^2}=1$. **OR**

b) Find the vertex, focus and equation of directrix of the parabola $y^2-4y-8x+12=0$.

47. a) Show that $p \leftrightarrow q \equiv ((\neg p) \vee q) \wedge ((\neg q) \vee p)$ **OR**

b) Solve the following system of linear equations by Cramer's Rule.

$\frac{3}{x}-\frac{4}{y}-\frac{2}{z}-1=0, \frac{1}{x}+\frac{2}{y}+\frac{1}{z}-2=0, \frac{2}{x}-\frac{5}{y}-\frac{4}{z}+1=0.$

GOVT. QUESTION PAPER- JUNE 2024

12TH STANDARD – MATHEMATICS

Time Allowed :3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

1. If in 6 trials, X is a binomial variable which follows the relation $9P(X=4)=P(X=2)$, then the probability of success is: (a) 0.125 (b) 0.25 (c) 0.375 (d) 0.75
2. If f $(x)=\int_0^x t\cot t\,dt$, then $\frac{df}{dx}$ =
   (a) $\cos x - x\sin x$ (b) $\sin x + x\cos x$ (c) $x\cos x$ (d) $x\sin x$
3. The value of the limit $\lim_{x\to 0}\left(cot\ x-\frac{1}{x}\right)$ is:
   (a) 0 (b) 1 (c) 2 (d) ∞
4. If x + y = k is a normal to the parabola $y^2 = 12x$, then the value of k is:
   (a) 3 (b) -1 (c) 1 (d) 9
5. The polynomial $x^3 - kx^2 + 9x$ has three real zeros if any only if, k satisfies:
   (a) $|k| \le 6$ (b) $k = 0$ (c) $|k| > 6$ (d) $|k| \ge 6$
6. If $A^T A^{-1}$ is symmetric, then A^2 = (a) A^{-1} (b) $(A^T)^2$ (c) A^T (d) $(A^{-1})^2$
7. The principal argument of $\frac{3}{-1+i}$ is: (a) $\frac{-5\pi}{6}$ (b) $\frac{-2\pi}{3}$ (c) $\frac{-3\pi}{4}$ (d) $\frac{-\pi}{2}$
8. The domain of the function defined by $f(x) = \sin^{-1}\sqrt{x-1}$ is:
   (a) [1,2] (b) [-1,1] (c) [0,1] (d) [-1,0]

9. If $\vec{a} = \hat{\imath} + \hat{\jmath} + \hat{k},\ \vec{b} = \hat{\imath} + \hat{\jmath},\ \vec{c} = \hat{\imath}$ and $(\vec{a} \times \vec{b}) \times \vec{c} = \lambda\vec{a} + \mu\vec{b}$, then the value of $\lambda + \mu$ is:

(a) 0 (b) 1 (c) 6 (d) 3

10. The order and degree of the differential equation $\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^{1/3} + x^{1/4} = 0$ are respectively:

(a) 2,3 (b) 3,3 (c) 2,6 (d) 2,4

11. The point of inflection of the curve y = $(x-1)^3$ is:

(a) (0,0) (b) (0,1) (c) (1,0) (d) (1,1)

12. If a compound statement involves 3 simple statements, then the number of rows in the truth table is: (a) 9 (b) 8 (c) 6 (d) 3

13. If A = $\begin{bmatrix} 7 & 3 \\ 4 & 2 \end{bmatrix}$, then $9I_2 - A =$ (a) A^{-1} (b) $\frac{A^{-1}}{2}$ (c) $3A^{-1}$ (d) $2A^{-1}$

14. The radius of the circle $3x^2 + by^2 + 4bx - 6by + b^2 = 0$ is : (a) 1 (b) 3 (c) $\sqrt{10}$ (d) $\sqrt{11}$

15. The value of $\int_{-1}^{2} |x|\, dx$ is: (a) $\frac{1}{2}$ (b) $\frac{3}{2}$ (c) $\frac{5}{2}$ (d) $\frac{7}{2}$

16. If f (x, y, z) = xy + yz + zx then $f_x - f_z$ is equal to:

(a) z – x (b) y –z (c) $x - z$ (d) $y - x$

17. If $\sin x$ is the integrating factor of the linear differential equation $\frac{dy}{dx} + Py = Q$, then P is:

(a) $\log \sin x$ (b) $\cos x$ (c) $\tan x$ (d) $\cot x$

18. Distance from the origin to the plane $3x - 6y + 2z + 7 = 0$ is:

(a) 0 (b) 1 (c) 2 (d) 3

19. The value of $\sin^{-1}(\cos x), 0 \le x \le \pi$ is:

(a) $\pi - x$ (b) $x - \frac{\pi}{2}$ (c) $\frac{\pi}{2} - x$ (d) $x - \pi$

20. If z = $\frac{(\sqrt{3}+i)^3 (3i+4)^2}{(8+6i)^2}$, then $|z|$ is equal to: (a) 0 (b) 1 (c) 2 (d) 3

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. Find z^{-1}, if $z = (2 + 3i)(1 - i)$.

22. Show that the equation $2x^2 - 6x + 7 = 0$ cannot be satisfied by any real values of x.

23. Show that $F(x, y) = \frac{x^2+5xy-10y^2}{3x+7y}$ is a homogeneous function of degree 1.

24. Form the differential equation by eliminating the arbitrary constants A and B from $y = A\cos x + B\sin x$.

25. If $dj(A) = \begin{bmatrix} 0 & -2 & 0 \\ 6 & 2 & -6 \\ -3 & 0 & 6 \end{bmatrix}$, find A^{-1}.

26. Obtain the equation of the circle for which (3,4) and (2,-7) are the ends of a diameter.

27. If X is the random variable with distribution function $F(x)$ given by,

$F(x) = \begin{cases} 0 & x < 0 \\ x & 0 \le x < 1 \\ 1 & 1 \le x \end{cases}$ then find the probability density function $f(x)$.

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28. Find the value of $\tan^{-1}\left(\tan\frac{5\pi}{4}\right)$.
29. Prove that the function $f(x) = x^2 - 2x - 3$ is strictly increasing in $(2, \infty)$.
30. The volume of the parallelepiped whose coterminous edges are $7\hat{\imath} + \lambda\hat{\jmath} - 3\hat{k}, \hat{\imath} + 2\hat{\jmath} - \hat{k}$, $-3\hat{\imath} + 7\hat{\jmath} + 5\hat{k}$ is 90 cubic units. Find the value of λ.

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Find the rank of the matrix $\begin{bmatrix} 3 & -8 & 5 & 2 \\ 2 & -5 & 1 & 4 \\ -1 & 2 & 3 & -2 \end{bmatrix}$.
32. Find the equation of the ellipse whose foci $(\pm 3, 0)$ and $e = \frac{1}{2}$.
33. A particle moves so that the distance moved is according to the law $s(t) = \frac{t^3}{3} - t^2 + 3$. At what time the velocity and acceleration are zero?
34. Prove that $q \to p \equiv \neg p \to \neg q$.
35. Find the square roots of $-6 + 8i$.
36. Find the Vector and Cartesian equations of the plane passing through the point with position vector $2\hat{\imath} + 6\hat{\jmath} + 3\hat{k}$ and normal to the vector $\hat{\imath} + 3\hat{\jmath} + 5\hat{k}$.
37. Solve: $(1 + x^2)\frac{dy}{dx} = 1 + y^2$.
38. Show that the percentage error in the n^{th} root of a number is approximately $\frac{1}{n}$ times the percentage error in the number.
39. Find a polynomial equation of minimum degree with rational coefficients, having $2i + 3$ as a root.
40. Evaluate : $\int_0^3 (3x^2 - 4x + 5)\, dx$

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Solve the following system of linear equations by matrix inversion method.
$2x + 3y - z = 9, x + y + z = 9, 3x - y - z = -1$ **OR**
b) Find the area of the region bounded between the parabolas $y^2 = 4x$ and $x^2 = 4y$.
42. a) If $\tan^{-1} x + \tan^{-1} y + \tan^{-1} z = \pi$, show that $x + y + z = xyz$. **OR**
b) Find centre, foci and vertices of the hyperbola $9x^2 - y^2 - 36x - 6y + 18 = 0$.

43. a) Find the angle between the rectangular hyperbola $xy = 2$ and the parabola $x^2 + 4y = 0$.
OR
b) Prove by vector method that $\cos(\alpha - \beta) = \cos\alpha\cos\beta + \sin\alpha\sin\beta$.
44. a) If $\vec{a} = \hat{\imath} - \hat{\jmath}, \vec{b} = \hat{\imath} - \hat{\jmath} - 4\hat{k}, \vec{c} = 3\hat{\jmath} - \hat{k}$ and $\vec{d} = 2\hat{\imath} + 5\hat{\jmath} + \hat{k}$, verify that
$(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = [\vec{a}, \vec{b}, \vec{d}]\vec{c} - [\vec{a}, \vec{b}, \vec{c}]\vec{d}$ **OR**
b) Find the population of a city at any time *t*, given that the rate of increase of population is proportional to the population at that instant and that in a period of 40 years the population increased from 3,00,000 to 4,00,000.

45. a) A bridge has a parabolic arch that is $10m$ high in the centre and $30m$ wide at the bottom. Find the height of the arch $6m$ from the centre, on either sides. **OR**

b) The mean and variance of a binomial variate *X* are respectively 2 and 1.5. Find
(i) $P(X = 0)$ (ii) $P(X = 1)$ (iii) $P(X \geq 1)$

46. a) Evaluate $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x}+\sqrt{x}} dx$ **OR**

b) Verify (i) Closure property (ii) Commutative property (iii) Associative property (iv) Existence of identity and (v) Existence of inverse for the operation X_{11} on a subset $A = \{1,3,4,5,9\}$of the set of remainders $\{0,1,2,3,4,5,6,7,8,9,10\}$.

47. a) If $z = x + iy$ and $\arg\left(\frac{z-1}{z+1}\right) = \frac{\pi}{2}$, show that $x^2 + y^2 = 1$. **OR**

b) Prove that among all the rectangles of the given perimeter, the square has the maximum area.

GOVT. QUESTION PAPER- MARCH 2025

12TH STANDARD – MATHEMATICS

Time Allowed :3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.

(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. An ellipse has OB as semi minor axes, F and F' its foct and the angle FBF' is a right angle. Then the eccentricity of the ellipse is:
(a) $\frac{1}{4}$ (b) $\frac{1}{\sqrt{2}}$ (c) $\frac{1}{\sqrt{3}}$ (d) $\frac{1}{2}$
2. The volume of the parallelepiped with its edges represented by the vectors $\hat{\imath} + \hat{\jmath}, \hat{\imath} + 2\hat{\jmath}, \hat{\imath} + \hat{\jmath} + \pi\hat{k}$ is: (a) π (b) $\frac{\pi}{2}$ (c) $\frac{\pi}{4}$ (d) $\frac{\pi}{3}$
3. If $u(x, y) = e^{x^2+y^2}$, then $\frac{\partial u}{\partial x}$ is equal to:
(a) x^2u (b) $e^{x^2+y^2}$ (c) y^2u (d) $2xu$
4. Subtraction is not a binary operation in: (a) $\mathbb{N}$ (b) $\mathbb{R}$ (c) $\mathbb{Q}$ (d) $\mathbb{Z}$
5. If A is a non-singular matrix of order 3×3 and $|A| = 5$ then $|A^{-1}|$ is :
(a) 5^2 (b) 5 (c) $\frac{1}{5^2}$ (d) $\frac{1}{5}$
6. The point of inflection of the curve y = $(x-1)^3$ is :
(a) (1,0) (b) (0,0) (c) (1,1) (d) (0,1)
7. A stone is thrown up vertically. The height it reaches at time t seconds is given by x = 80t -16t^2 The stone reaches the maximum height in time t seconds is given by:
(a) 3 (b) 2 (c) 3.5 (d) 2.5
8. If f(x) > 0 for all x and g(x) = log(f(x)), then dg is:

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(a) $\frac{1}{f(x)}\,dx$ (b) $\frac{1}{f(x)}f'(x)\,dx$ (c) $\frac{1}{x}\,dx$ (d) $\frac{1}{x}f(x)\,dx$

9. The domain of the function defined by f(x) = $\sin^{-1}\sqrt{x-1}$ is:
   (a) [0,1] (b)[1,2] (c) [-1,0] (d) [-1,1]
10. Suppose that X takes on one of the values 0, 1 and 2. If for some constant k, P(X = i) = k P(X = i – 1) for i =1, 2 and P(X = 0)= $\frac{1}{7}$, then the value of k is:
    (a)1 (b) 2 (c) 3 (d) 4
11. The volume of solid of revolution of the region bounded by $y^2 = x(a-x)$about x axis is:
    (a) $\frac{\pi a^3}{5}$ (b) πa^3 (c) $\frac{\pi a^3}{6}$ (d) $\frac{\pi a^3}{4}$
12. The order and degree of differential equation $\sqrt{\frac{dy}{dx}} - 4\frac{dy}{dx} - 7x = 0$ are respectively:
    (a)1, 2 (b) 2, 1 (c) 2,2 (d) 1, 1
13. The value of $\int_0^{\frac{2}{3}} \frac{dx}{\sqrt{4-9x^2}}$ is:
    (a) $\frac{\pi}{4}$ (b) $\frac{\pi}{6}$ (c) π (d) $\frac{\pi}{2}$
14. If A = $\begin{bmatrix} 2 & 3 \\ 5 & -2 \end{bmatrix}$ be such that λA^{-1} = A, then λ is:
    (a)19 (b) 17 (c) 21 (d) 14
15. The value of $\sum_{i=1}^{13}(i^n + i^{n-1})$ is:
    (a) 1 (b) 1 +i (c) 0 (d) i
16. The angle between the lines $\frac{x-2}{3} = \frac{y+1}{-2}, z = 2$ and $\frac{x-1}{1} = \frac{2y+3}{3} = \frac{z+5}{2}$ is:
    (a) $\frac{\pi}{3}$ (b) $\frac{\pi}{6}$ (c) $\frac{\pi}{2}$ (d) $\frac{\pi}{4}$
17. The square root if i are:
    (a)$\pm\frac{1}{2}(1+i)$ (b)$\pm\frac{1}{\sqrt{2}}(1+i)$ (c)$\pm\frac{1}{2}(1-i)$ (d) $\pm\frac{1}{\sqrt{2}}(1-i)$
18. The slope at any point of a curve y = f(x) is given by $\frac{dy}{dx} = 3x^2$ and it passes through (-1,1). Then the equation of the curve is:
    (a) y = $3x^3$+4 (b) y = x^3+2 (c) y = x^3+5 (d) y = $3x^2$+4
19. If in 6 trials, X is a binomial variable which follows the relation $9P(X=4) = P(X=2)$, then the probability of success is:
    (a) 0.375 (b) 0.125 (c)0.75 (d) 0.25
20. The number of real numbers in [0, 2π] satisfying $\sin^4 x - 2\sin^2 x + 1$ is
    (a) 1 (b) 2 (c) ∞ (d) 4

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

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21. If adjA $= \begin{bmatrix} -1 & 2 & 2 \\ 1 & 1 & 2 \\ 2 & 2 & 1 \end{bmatrix}$, find A^{-1}.
22. If $= x + iy$, then find $Re\left(\frac{1}{z}\right)$ in rectangular form.
23. Find the value of $\tan^{-1}\left(-\sqrt{3}\right)$.
24. If $y = 4x + c$ is a tangent to the circle $x^2 + y^2 = 9$, find c.
25. Find the slant (oblique) asymptote for the function $f(x) = \frac{x^2-6x+7}{x+5}$.
26. Show that $F(x, y) = \frac{x^2+5xy-10y^2}{3x+7y}$ is a homogeneous function of degree 1.
27. Solve $\frac{dy}{dx} = \sqrt{\frac{1-y^2}{1-x^2}}$
28. Find the constant *C* such that the function $f(x) = \begin{cases} Cx^2 & 1 < x < 4 \\ 0 & \text{otherwise} \end{cases}$ is a density function of X.
29. Find a polynomial equation of minimum degree with rational coefficients having i-2 as a root.
30. If $f(x) = \sin x$, then prove that $\int_0^{\pi} f(x)dx = 2\int_0^{\frac{\pi}{2}} f(x)dx$

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Solve the system of linear equations $2x + 5y = -2, x + 2y = -3$ by matrix inversion method.
32. If $|z| = 2$, show that $8 \leq |z + 6 + 8i| \leq 12$
33. Solve the equation $7x^3 - 43x^2 = 43x - 7$
34. Prove that $\tan^{-1}\frac{2}{11} + \tan^{-1}\frac{7}{24} = \tan^{-1}\frac{1}{2}$
35. If $\vec{a}, \vec{b}, \vec{c}$ are three vectors, prove that $\left[\vec{a} + \vec{c}, \vec{a} + \vec{b}, \vec{a} + \vec{b} + \vec{c}\right] = \left[\vec{a}, \vec{b}, \vec{c}\right]$
36. If $u(x, y) = x^2y + 3xy^4, x = e^t$ and $= \sin t$, find $\frac{du}{dt}$
37. Evaluate $\int_0^{\frac{\pi}{2}} \frac{dx}{1+5\cos^2 x}$
38. A lottery with 600 tickets gives one prize of `200, four prizes of `100, and six prizes of `50. If the ticket costs is `2, find the expected winning amount of a ticket.
39. Find the Taylor's series about $x = 2$ for $f(x) = x^3 + 2x + 1, (-\infty < x < \infty)$
40. Let Q be the set of all Rational numbers. If * is a binary operation defined on Q as $a * b = a + b - ab + 7$ and $\left(\frac{3}{2}\right) * m = \frac{87}{10}$, then find the value of m.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. (a) Solve, by Cramer's rule, the system of equations $x_1 - x_2 = 3,\ 2x_1 + 3x_2 + 4x_3 = 17,$ $x_2 + 2x_3 = 7$ **OR**

    (b) Find the equation of tangent and normal to the curve given by $x = 7\cos t$ and $y = 2\sin t, t \in \mathbb{R}$ at any point on the curve.

42. (a) If $\omega \neq 1$ is a cube root of unity, show that the roots of the equation $(z-1)^3 + 8 = 0$ are

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$-1, 1-2\omega, 1-2\omega^2$. **OR**

(b) Find the area of the region bounded by the parabola $y^2 = x$ and the line $y = x - 2$

43. (a) Solve the equation $6x^4 - 5x^3 - 38x^2 - 5x + 6 = 0$ if it is known that $\frac{1}{3}$ is a solution.

OR

(b) Solve $(x^2 - 3y^2)dx + 2xydy = 0$.

44. (a) A bridge has a parabolic arch that is $10m$ high in the centre and $30m$ wide at the bottom. Find the height of the arch $6m$ from the centre, on either sides. **OR**

(b) Using vector method, prove that $\cos(\alpha - \beta) = \cos\alpha\cos\beta + \sin\alpha\sin\beta$.

45. (a) During war,1 ship out of 9 was sunk on an average in making a certain voyage. What was the probability that:

(i) Exactly 3 out of a convoy of 6 ships would arrive safely?

46. (ii) No ships arrive safely from a convoy of 4 ships. **OR**

(b) Find the equation of the ellipse whose foci are (2, 1), (-2, 1) and length of the latus rectum is 6.

47. (a) Find the non-parametric form of vector equation, and Cartesian equation of the plane passing through the point $(0,1,-5)$ and parallel to the straight lines

$\vec{r} = (\hat{\imath} + 2\hat{\jmath} - 4\hat{k}) + s(2\hat{\imath} + 3\hat{\jmath} + 6\hat{k})$ and $\vec{r} = (\hat{\imath} - 3\hat{\jmath} + 5\hat{k}) + t(\hat{\imath} + \hat{\jmath} - \hat{k})$. **OR**

(b) The growth of a population is proportional to the number present. If the population of a colony doubles in 50 years, in how many years will the population become triple?

48. (a) A hollow cone with base radius $a\ cm$ and height $b\ cm$ is placed on a table. Show that the volume of the largest cylinder that can be hidden underneath is $\frac{4}{9}$ times volume of the cone. **OR**

(b) Using truth table, prove that p ∧ (q∨r) ≡ (p ∧ q) ∨ (p ∧ r)

GOVT. QUESTION PAPER- JUNE 2025

12TH STANDARD – MATHEMATICS

Time Allowed :3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.

(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. If A = $\begin{bmatrix} cos\theta & sin\theta \\ -sin\theta & cos\theta \end{bmatrix}$ and A(adjA) = $\begin{bmatrix} k & 0 \\ 0 & k \end{bmatrix}$, then k =

(a) 0 (b) $\sin\theta$ (c) $\cos\theta$ (d) 1

2. If $|z| = 1$, then the value of $\frac{1+z}{1+\bar{z}}$ is:

(a) z (b) $\bar{z}$ (c) $\frac{1}{z}$ (d) 1

3. The polynomial $x^3 - kx^2 + 9x$ has three real zeros if any only if, k satisfies.

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(a) $|k| \leq 6$ (b) $k = 0$ (c) $|k| > 6$ (d) $|k| \geq 6$

4. If $\sin^{-1} x + \sin^{-1} y = \frac{2\pi}{3}$; then $cos^{-1}\, x + cos^{-1}\, y$ is equal to:

(a) $\frac{2\pi}{3}$ (b) $\frac{\pi}{3}$ (c) $\frac{\pi}{6}$ (d) π

5. The radius of the circle $3x^2 + by^2 + 4bx - 6by + b^2 = 0$ is:

(a)1 (b) 3 (c) $\sqrt{10}$ (d) $\sqrt{11}$

6. Let A be a non-singular square matrix of order *n*. Which one of the following is incorrect?

(a) adj(adjA) = $|A|^{n-2}$ A (b) $|adjA| = A^{n-1}$ (c) |adj(adjA)| = $|A|^{(n-1)^2}$ (d) $(adjA)^T = adj(A^T)$

7. $cis\left(\frac{28\pi}{5}\right)$ is equal to: (a) $cis\left(\frac{-2\pi}{5}\right)$ (b) $cis\left(\frac{2\pi}{5}\right)$ (c) $cis\left(\frac{3\pi}{5}\right)$ (d) $cis\left(\frac{-3\pi}{5}\right)$

8. If $\vec{a}$ and $\vec{b}$ are unit vectors such that $[\vec{a}, \vec{b}, \vec{a} \times \vec{b}] = \frac{1}{4}$, then the angle between $\vec{a}$ and $\vec{b}$ is:

(a) $\frac{\pi}{6}$ (b) $\frac{\pi}{4}$ (c) $\frac{\pi}{3}$ (d) $\frac{\pi}{2}$

9. If $\vec{a} = 2\hat{\imath} + 3\hat{\jmath} - \hat{k}$, $\vec{b} = \hat{\imath} + 2\hat{\jmath} - 5\hat{k}$, $\vec{c} = 3\hat{\imath} + 5\hat{\jmath} - \hat{k}$, then a vector perpendicular to $\vec{a}$ and lies in the plane containing $\vec{b}$ and $\vec{c}$ is:

(a) $-17\hat{\imath} + 21\hat{\jmath} - 97\hat{k}$ (b) $17\hat{\imath} + 21\hat{\jmath} - 123\hat{k}$

(c) $-17\hat{\imath} - 21\hat{\jmath} + 97\hat{k}$ (d) $-17\hat{\imath} - 21\hat{\jmath} - 97\hat{k}$

10. The tangent to the curve $y^2 - xy + 9 = 0$ is vertical when:

(a) y = 0 (b) $y = \pm\sqrt{3}$ (c) $y = \frac{1}{2}$ (d) $y = \pm 3$

11. The number given by the Mean value theorem for the function $\frac{1}{x}$, $x \in [1, 9]$ is:

(a) 2 (b) 2.5 (c) 3 (d) 3.5

12. If $w(x, y) = x^y$, $x > 0$, then $\frac{\partial w}{\partial x}$ is equal to:

(a) $x^y \log x$ (b) $y \log x$ (c) yx^{y-1} (d) $x \log y$

13. The value of $\int_{-1}^{2} |x|\, dx$ is:

(a) $\frac{1}{2}$ (b) $\frac{3}{2}$ (c) $\frac{5}{2}$ (d) $\frac{7}{2}$

14. If $\int_o^x f(t)dt = x + \int_x^1 tf(t)dt$, then the value of f (1) is:

(a) $\frac{1}{2}$ (b) 2 (c) 1 (d) $\frac{3}{4}$

15. The solution of $\frac{dy}{dx} + p(x)y = 0$ is:

(a) $y = ce^{\int p dx}$ (b) $y = ce^{-\int p dx}$ (c) $x = ce^{-\int p dy}$ (d) $x = ce^{\int p dy}$

16. If $P(X = 0) = 1 - P(X = 1)$. If $E(X) = 3\mathrm{Var}(X)$, then $P(X = 0)$ is:

(a) $\frac{2}{3}$ (b) $\frac{2}{5}$ (c) $\frac{1}{5}$ (d) $\frac{1}{3}$

17. Let X have a Bernoulli distribution with mean 0.4, then the variance of $(2X - 3)$ is:

(a) 0.24 (b) 0.48 (c) 0.6 (d) 0.96

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18. Which one is the inverse of the statement $(p \vee q) \rightarrow (p \wedge q)$?

(a) $(p \wedge q) \rightarrow (p \vee q)$ (b) $\neg(p \vee q) \rightarrow (p \wedge q)$

(c) $(\neg p \vee \neg q) \rightarrow (\neg p \wedge \neg q)$ (d) $(\neg p \wedge \neg q) \rightarrow (\neg p \vee \neg q)$

19. If f(x) = x is an identity function then the differential df is :

(a) dy (b) dx (c) –dy (d) –dx

20. The order and degree of the differential equation $3\left(\frac{d^2y}{dx^2}\right) = \left[4 + \left(\frac{dy}{dx}\right)^2\right]^{\frac{3}{2}}$ are:

(a) 2,1 (b) 2,2 (c) 3, 3 (d) 3,2

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. Prove that $\begin{bmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{bmatrix}$ is orthogonal matrix.
22. Simplify : $i^{1947} + i^{1950}$
23. Solve : $x^4 - 5x^2 + 6 = 0$
24. Find the value of $\cos^{-1}\left(\cos\left(\frac{7\pi}{6}\right)\right)$
25. Find centre and radius of the circle $x^2 + y^2 - x + 2y - 3 = 0$.
26. Evaluate: $\lim_{x\to\infty} \frac{x^2+17x+29}{x^4}$.
27. If $W(x, y, z) = x^2y + y^2z + z^2x,\ x, y, z \in R$, find the differential dw.
28. Form the differential equation by eliminating the arbitrary constants A and B from $y = A\cos x + B\sin x$.
29. Three fair coins are tossed simultaneously. Find the probability mass function for number of heads occurred.
30. $\int_0^a \frac{dx}{9+x^2} = \frac{\pi}{12}$ then find 'a'.

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Solve the following system of linear equations, using matrix inversion method. $2x - y = 8, 3x + 2y = -2$
32. If $z = x + iy$ is a complex number such that $\left|\frac{z-4i}{z+4i}\right| = 1$ show that the locus of z is real axis.
33. Solve the equation $\sin^2 x - 5\sin x + 4 = 0$
34. Prove that $2\tan^{-1}\left(\frac{1}{2}\right) + \tan^{-1}\left(\frac{1}{7}\right) = \tan^{-1}\left(\frac{31}{17}\right)$
35. Find the absolute maximum and absolute minimum of the function $f(x) = 2x^3 - 3x^2 - 12x + 5$ on $[-2,4]$
36. Show that the points $(2,3,4), (-1,4,5)$ and $(8,1,2)$ are collinear.
37. If the radius of a sphere, with radius $10\ cm$, has to decrease by $0.1cm$, approximately how much will its volume decrease?

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38. Evaluate: $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x}+\sqrt{x}}dx$

39. Two balls are chosen randomly from an urn containing 6 white and 4 black balls. Suppose that we win ₹30 for each black ball selected and we lose ₹20 for each white ball selected. If X denotes the winning amount, find the values of X and number of points in its inverse images.

40. On Z^+, define an operation $*$ by (a$*$b) = a^b + ab , $\forall$ a, b $\in Z^+$. Is $*$ a binary operation on Z^+ ? If so , find a when a$*$2 = 8.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. (a) Solve the following system of linear equations, by Gaussian elimination method :
$4x + 3y + 6z = 25, x + 5y + 7z = 13, 2x + 9y + z = 1$ **OR**

(b) Prove that the ellipse $x^2 + 4y^2 = 8$ and the hyperbola $x^2 - 2y^2 = 4$ intersect orthogonally.

42. (a) Show that $\left(\frac{19-7i}{9+i}\right)^{12} + \left(\frac{20-5i}{7-6i}\right)^{12}$ is real. **OR**

(b) Find the area of the region in the first quadrant bounded by the parabola $y^2 = 4x$, the line $x + y = 3$ and y -axis.

43. (a) Prove by vector method that $\sin(\alpha + \beta) = \sin\alpha\cos\beta + \cos\alpha\sin\beta$. **OR**

(b) Solve $\frac{dy}{dx} + \frac{y}{x\log x} = \frac{\sin 2x}{\log x}$.

44. (a) Find the non-parametric form of vector equation and cartesian equation of the plane passing through the point $(1, -2, 4)$ and perpendicular to the plane $x + 2y - 3z = 11$ and parallel to the line $\frac{x+7}{3} = \frac{y+3}{-1} = \frac{z}{1}$. **OR**

(b) A garden is to be laid out in a rectangular area and protected by wire fence. What is the largest possible area of the fenced garden with 40 metres of wire.

45. (a) Solve the following equation. $x^4 - 10x^3 + 26x^2 - 10x + 1 = 0$.

(b) A semielliptical archway over a one-way road has a height of $3m$ and a width of $12m$. The truck has a width of $3m$ and a height of $2.7m$. Will the truck clear the opening of the archway?

46. (a) Suppose a person deposits `10,000 in a bank account at the rate of 5% per annum compounded continuously. How much money will be in his bank account 18 months later? **OR**

(b) Prove that $p \to (\neg q \vee r) \equiv \neg p \vee (\neg q \vee r)$ using truth table.

47. (a) A random variable X has the following probability mass function.

x	1	2	3	4	5	6	7
f(x)	k	2k	3k	2k	k^2	$2k^2$	$7k^2$+k

(i) Find 'k' (ii) Evaluate P(X < 4) (iii) Evaluate P(2 < X < 6)

(iv) If P(X $\leq$ x) > $\frac{1}{2}$, then find the minimum value of x. **OR**

(b) Find the centre, vertices and foci of the ellipse $13x^2 + 49y^2 + 182x - 98y + 49 = 0$.

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GOVT. QUESTION PAPER- MARCH 2026

12TH STANDARD – MATHEMATICS

Time Allowed :3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.

(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. If f and g are polynomials of degree m and n respectively and if h(x) = (f·g)(x), then the degree of h is: (a) m^n (b) mn (c) n^m (d) m+n
2. If x < 0 , then $tan^{-1}\left(\frac{1}{x}\right)$ is equal to :
   (a) $-\pi + \cot^{-1} x$ (b) $\tan^{-1} x$ (c) $-\pi + \tan^{-1} x$ (d) $\cot^{-1} x$
3. One of the closest points the curve $x^2 - y^2 = 4$ to the point (6,0) is:
   (a) $\left(3, \sqrt{5}\right)$ (b) (2,0) (c) $\left(\sqrt{13}, -\sqrt{3}\right)$ (d) $\left(\sqrt{5}, 1\right)$
4. The solution of the differential equation $2x\frac{dy}{dx} - y = 3$ represents :
   (a) Parabola (b) Straight lines (c) Ellipse (d) Circles
5. P is the amount of certain substance left in after time t . If the rate of evaporation of the substance is proportional to the amount remaining, then :
   (a) P = Ckt (b) $P = Ce^{kt}$ (c) Pt = C (d) $P = Ce^{-kt}$
6. If the image of the point A(1,2,3) with respect to the plane $\vec{r}.\left(\hat{\imath} + 2\hat{\jmath} + 4\hat{k}\right) = 38$ is $A'(3,6,11)$, then the foot of the perpendicular from the point A to the given plane is :
   (a) (2,5,7) (b) (2,3,7) (c) (2,-4,7) (d) (2,4,7)
7. If a vector $\vec{\alpha}$ lies in the plane of $\vec{\beta}$and $\vec{\gamma}$, then
   (a) $[\vec{\alpha},\vec{\beta},\vec{\gamma}] = 0$ (b) $[\vec{\alpha},\vec{\beta},\vec{\gamma}] = 1$ (c) $[\vec{\alpha},\vec{\beta},\vec{\gamma}] = 2$ (d) $[\vec{\alpha},\vec{\beta},\vec{\gamma}] = -1$
8. A rod of length $2l$ is broken into two pieces at random. The probability density function of the shorter of the two pieces is $f(x) = \begin{cases} \frac{1}{l} & 0 < x < l \\ 0 & l \le x < 2l \end{cases}$

   The mean and variance of the shorter of the two pieces are respectively :
   (a) $l, \frac{l^2}{12}$ (b) $\frac{l}{2}, \frac{l^2}{3}$ (c) $\frac{l}{2}, \frac{l^2}{12}$ (d) $\frac{l}{2}, \frac{l^2}{6}$
9. The product of all four values of $\left[cos\frac{\pi}{3} + i\, sin\frac{\pi}{3}\right]^{\frac{3}{4}}$ is :
   (a) 1 (b) -2 (c) 2 (d) -1
10. If $f(x) = \int_0^x t\cot t\, dt$, then $\frac{df}{dx} =$
    (a) $x\cos x$ (b) $\cos x - x\sin x$ (c) $x\sin x$ (d) $\sin x + x\cos x$
11. The percentage error of fifth root of 31 is approximately how many times the percentage error in 31?

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(a) 5 (b) $\frac{1}{31}$ (c) 31 (d) $\frac{1}{5}$

12. The dual of $\neg(p \vee q) \vee [p \vee (p \wedge \neg r)]$ is :

(a) $\neg (p \wedge q) \wedge [p \wedge (p \wedge r)]$ (b) $\neg (p \wedge q) \wedge [p \vee (p \wedge \neg r)]$

(c) $\neg (p \wedge q) \wedge [p \wedge (p \vee \neg r)]$ (d) $(p \wedge q) \wedge [p \wedge (p \vee \neg r)]$

13. The value of 'c' satisfied by the Rolle's theorem for the function f(x) = $x^3 - 3x^2$, $x \in [0,3]$ is : (a) $\frac{3}{2}$ (b) 1 (c) 2 (d) $\sqrt{2}$

14. If A is a 3×3 non-singular matrix such that $AA^T = A^TA$ and $B = A^{-1}A^T$, then $BB^T =$

(a) I_3 (b) A (c) B^T (d) B

15. If $\rho(A) = \rho([A \setminus B])$, then the AX = B of linear equations is :

(a) consistent and has infinitely many solution

(b) consistent and has a unique solution

(c) inconsistent (d) consistent

16. The eccentricity of the circle is:

(a) $\frac{1}{2}$ (b) 0 (c) 2 (d) 1

17. If the function $f(x) = \frac{1}{12}$ for $a < x < b$, represents a probability density function of a continuous random variable X, then which of the following cannot be the value of a and b? (a) 7 and 19 (b) 0 and 12 (c) 16 and 24 (d) 5 and 17

18. Let A = {(x,y) / a < x < b, c < y < d } $\subset \mathbb{R}^2$. If the function u : A$\rightarrow \mathbb{R}^2$ is harmonic in A, then :

(a) $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0 \ \forall$ (x,y) $\in$ A (b) $\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 1 \ \forall$ (x,y) $\in$ A

(c) $\frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial y^2} = 0 \ \forall$ (x,y) $\in$ A (d) $\frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial y^2} = 1 \ \forall$ (x,y) $\in$ A

19. If $f(x) = \int_1^x \frac{e^{\sin u}}{u} du, x > 1$ and $\int_1^3 \frac{e^{\sin x^2}}{x} dx = \frac{1}{2}[f(a) - f(1)]$, then one of the possible value of a is:

(a) 9 (b) 3 (c) 5 (d) 6

20. If z is a complex number such that z $\in \mathbb{C}\setminus\mathbb{R}$ and z + $\frac{1}{z} \in \mathbb{R}$, then $|z|$ is :

(a) 2 (b) 0 (c) 3 (d) 1

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. If A is a non-singular matrix of odd order, prove that $|adj\ A|$ is positive.

22. Simplify : $\sum_{n=1}^{12} i^n$

23. If $x^2 + 2(k+2)x + 9k = 0$ has equal roots, find k.

24. Simplify : $\sin^{-1}[\sin 10]$

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25. Obtain the equation of the circles with radius 5 cm and touching *x*-axis at the origin in general form.

26. Prove that the function $f(x) = x^2 - 2x - 3$ is strictly increasing in $(2, \infty)$

27. If f(x,y) = $cos^{-1}\left(\frac{x}{y}\right)$, then show that $f_y = \frac{x}{y\sqrt{y^2-x^2}}$

28. Evaluate : $\int_0^{\frac{\pi}{2}} \sin^{10} x\, dx$

29. Determine the order and degree (if exists) of the following differential equation

$$x^2 \frac{d^2y}{dx^2} + \left[1 + \left(\frac{dy}{dx}\right)^2\right]^{\frac{1}{2}} = 0$$

30. If $\sqrt{Var(X)} = \frac{1}{2}$ then, find the value of Var (2X + 3)

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Find the rank of the matrix $\begin{bmatrix} 2 & -2 & 4 & 3 \\ -3 & 4 & -2 & -1 \\ 6 & 2 & -1 & 7 \end{bmatrix}$ by reducing it to an echelon form.

32. Find all real numbers satisfying the equation : $4^x - 3(2^{x+2}) + 2^5 = 0$.

33. Prove that $2\tan^{-1}\frac{1}{2} + \tan^{-1}\frac{1}{7} = \tan^{-1}\frac{31}{17}$

34. Find the points where the straight line passes through $(6,7,4)$ and $(8,4,9)$ cuts the *xz* and *yz* planes.

35. If $\lim_{\theta \to 0}\left(\frac{1-\cos m\theta}{1-\cos n\theta}\right)$, then prove that $m = \pm n$.

36. Use the linear approximation to find approximate values of $\sqrt[4]{15}$

37. If $\int_0^\infty e^{-x}x^n dx$ = 5!, then find the value of $\int_0^\infty e^{-x}x^{n-1}dx$

38. If $X \sim B(n,p)$ such that $4P(X = 4) = P(X = 2)$ and $n = 6$. Find the distribution, mean and standard deviation of *X*.

39. Verify (i) Closure property (ii) Associative property and (iii) existence of identity for following operation on the given set: $m * n = m + n - mn;\ m, n \in Z$

40. If $z_1 = \overline{1 + i}$ and $\bar{z}_2 = 1 - i$, find the inverse of $\left(\frac{z_1}{z_2}\right)^{2026}$

PART-IV

Note: Answer **all** the questions. **7x5=35**

41.(a) Solve the following system of equations, using matrix inversion method.

$2x_1 + 3x_2 + 3x_3 = 5,\ x_1 - 2x_2 + x_3 = -4,\ 3x_1 - x_2 - 2x_3 = 3$ **OR**

(b) Show that the equation $z^3 + 2\bar{z} = 0$ has five solutions.

42. (a) Prove that $p \to (\neg q \vee r) \equiv \neg p \vee (\neg q \vee r)$ using truth table. **OR**

(b) Prove that $\int_0^{\frac{\pi}{4}} \log(1 + \tan x)dx = \frac{\pi}{8}\log 2$.

41.(a) Solve the equation $(x + 1)(x + 3)(x - 2)(x - 4) + 21 = 0$ **OR**

(b) Sketch the curve y = log(1+x)

44. (a) Show that the line $x - y + 4 = 0$ is a tangent to the ellipse $x^2 + 3y^2 = 12$. Also find the

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coordinates of the point of contact. **OR**

(b) Assume that the rate at which radioactive nuclei decay is proportional to the number of such nuclei that are present in a given sample. In a certain sample 10% of the original number of radioactive nuclei have undergone disintegration in a period of 100 years. What percentage of the original radioactive nuclei will remain after 1000 years?

45. (a) By vector method, prove that : $\cos(\alpha+\beta) = \cos\alpha\cos\beta - \sin\alpha\sin\beta$ **OR**

(b) $(x^2+y^2)dy = xydx$. It is given that $y(1) = 1$ and $y(x_0) = e$. Find the value of x_0 .

46. (a) A random variable *X* has the following probability mass function.

Find (i)$P(2 < X < 6)$ (ii)$P(2 \le X < 5)$ (iii)$P(X \le 4)$ (iv)$P(3 > X)$

x	1	2	3	4	5	6
f (x)	*k*	2*k*	6*k*	5*k*	6*k*	10k

OR

(b) At a water fountain, water attains a maximum height of $4m$ at horizontal distance of $0.5m$ from its origin. If the pathof water is a parabola, find the height of water at a horizontal distance of $0.75m$ from the point of origin.

47. (a) A particle moves along a line according to the law $s(t) = 2t^3 - 9t^2 + 12t - 4$, where ≥ 0 .

(i) At what times the particle changes direction?

(ii) Find the total distance travelled by the particle in the first 4 seconds.

(iii) Find the particle's acceleration each time the velocity is zero. **OR**

(b) Find the non-parametric form of Vector equation and Cartesian equation of the plane passing through the point $(1,-2,4)$ and perpendicular to the plane $x+2y-3z=11$ and parallel to the line $\frac{x+7}{3} = \frac{y+3}{-1} = \frac{z}{1}$.

GOVT. QUESTION PAPER- JULY 2026

12TH STANDARD – MATHEMATICS

Time Allowed : 3.00 Hours **Max.Marks : 90**

PART – I **20x1 = 20**

Note: (i) Answer all the questions.

(ii) Choose the most appropriate answers from the given alternatives and write the option code and the corresponding answer.

1. If $|adj(adjA)| = |A|^9$, then the order of the square matrix A is:

(a) 3 (b) 4 (c) 2 (d) 5

2. If α and β are the roots of $x^2 + x + 1 = 0$, then $\alpha^{2020} + \beta^{2020}$ is:

(a) – 2 (b) – 1 (c) 1 (d) 2

3. The polynomial $x^3 - kx^2 + 9x$ has three real zeros if any only if, k satisfies :

(a) $|k| \leq 6$ (b) $k = 0$ (c) $|k| > 6$ (d) $|k| \geq 6$

4. If the function f(x) = $\sin^{-1}(x^2-3)$, then x belongs to:

(a) [-1,1] (b) $[\sqrt{2},2]$ (c) $[-2,-\sqrt{2}]\cup[\sqrt{2},2]$ (d) $[-2,-\sqrt{2}]$

5. Let C be the circle with centre at $(1,1)$ and radius $= 1$. If T is the circle centered at $(0,y)$ passing through the origin and touching the circle C externally, then the radius of T is equal:

(a) $\frac{\sqrt{3}}{\sqrt{2}}$ (b) $\frac{\sqrt{3}}{2}$ (c) $\frac{1}{2}$ (d) $\frac{1}{4}$

6. If the direction cosines of a line are $\frac{1}{c}, \frac{1}{c}, \frac{1}{c}$, then:

(a) c = ± 3 (b) c = $\pm\sqrt{3}$ (c) c > 0 (d) 0 < c < 1

7. The maximum value of the function f(x) = x^2e^{-2x} , x > 0 is:

(a) $\frac{1}{e}$ (b) $\frac{1}{2e}$ (c) $\frac{1}{e^2}$ (d) $\frac{4}{e^4}$

8. If f(x) = $\frac{x}{x+1}$,then its differential is given by :

(a) $\frac{-1}{(x+1)^2}$ dx (b) $\frac{1}{(x+1)^2}$ dx (c) $\frac{1}{x+1}$ dx (d) $\frac{-1}{x+1}$ dx

9. The value of $\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \left[\frac{2x^7-3x^5+7x^3-x+1}{cos^2x}\right] dx$is

(a) 4 (b) 3 (c) 2 (d) 0

10. The solution of the differential equation $\frac{dy}{dx} + \frac{1}{\sqrt{1-x^2}} = 0$ is :

(a) $y + \sin^{-1} x = c$ (b) $x + \sin^{-1} y = 0$

(c) $y^2 + 2\sin^{-1} x = C$ (d) $x^2 + 2\sin^{-1} y = 0$

11. If A = $\begin{bmatrix} 2 & 0 \\ 1 & 5 \end{bmatrix}$ and B = $\begin{bmatrix} 1 & 4 \\ 2 & 0 \end{bmatrix}$ then $|adj(AB)|$ =

(a) -40 (b) -80 (c) -60 (d) -20

12. The principal argument of the complex number $\frac{-10}{1+i\sqrt{3}}$ is :

(a) $-\pi$ (b) π (c) $\frac{2\pi}{3}$ (d) - $\frac{\pi}{3}$

13. The value of the limit $\lim_{x\to 0}\left(cot\ x - \frac{1}{x}\right)$ is:

(a) 0 (b) 1 (c) 2 (d) ∞

14. If $\int_0^a \frac{1}{4+x^2} dx = \frac{\pi}{8}$ then a is:

(a) 4 (b) 1 (c) 3 (d) 2

15. Which one of the following is not true?

(a) Negation of a negation of a statement is the statement itself.

(b) If the last column of the truth table contains only T then it is a tautology.

(c) If the last column of its truth table contains only F then it is a contradiction.

(d) If p and q are any two statements then $p \leftrightarrow q$ is a tautology.

16. $\hat{\imath} - 3\hat{\jmath} + 4\hat{k}$, $2\hat{\imath} - \hat{\jmath} + 3\hat{k}$ and m$\hat{\imath} + 2\hat{\jmath} + \hat{k}$ are coplanar, then the value of m is:

(a) 2 (b) -2 (c) 3 (d) -3

17. Let X represent the difference between the number of heads and the number of tails obtained when a coin is tossed n times. Then the possible values of X are :

(a) i+ 2n, i = 0,1,2…n (b) 2i – n, i = 0,1,2…n

(c) n- i, i = 0,1,2…n (d) 2i + 2n, i = 0,1,2….n

18. Which of the following is incorrect?

(a) If f is a constant function, then df = 0

(b) If f(x) = x identity function, then df = 1dx

(c) If f is differential and cϵR, then d(cf) = cf'(x)dx

(d) If f(x) < 0 for all x and g(x) = log(f(x)), then dg = $\frac{f'(x)}{f(x)}dx$

19. If $P(X = 0) = 1 - P(X = 1)$ and $E(X) = 3\text{Var}(X)$, then $P(X = 0)$ is:

(a) $\frac{2}{3}$ (b) $\frac{2}{5}$ (c) $\frac{1}{5}$ (d) $\frac{1}{3}$

20. Which one of the following differential equation has order 1 and degree 1?

(a) $e^{\frac{dy}{dx}} + \frac{dy}{dx} = 0$ (b) $y\left(\frac{dy}{dx}\right) = \frac{x}{\left(\frac{dy}{dx}\right)+\left(\frac{dy}{dx}\right)^3}$

(c) $\sqrt{cosx}$(dx-dy) - $\sqrt{sinx}$(dx+dy) = 0 (d) $\sqrt{\frac{dy}{dx}} - 4\frac{dy}{dx}$ -7x = 0

PART-II

Note: Answer **any seven** questions. Question No. **30 is compulsory**. **7x2=14**

21. Prove that $\begin{bmatrix}\cos\theta & -\sin\theta \\ \sin\theta & \cos\theta\end{bmatrix}$ is orthogonal.

22. Simplify$\left(\frac{1+i}{1-i}\right)^3 - \left(\frac{1-i}{1+i}\right)^3$ into rectangular form

23. Discuss the nature of the roots of the polynomial equation:

$x^{2018} + 1947x^{1950} + 15x^8 + 26x^6 + 2019 = 0$

24. Find the principal value of $\text{cosec}^{-1}(-1)$

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25. Prove that the length of Latus rectum of the parabola $y^2 = 4ax$ is 4a.

26. Explain why Rolle's theorem is not applicable to the functions $f(x) = \left|\frac{1}{x}\right|, x \in [-1,1]$

27. The radius of a circular plate is measured as 12.65cm instead of the actual length $12.5cm$. Find the absolute error in calculating the area of the circular plate.

28. Evaluate: $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x}+\sqrt{x}} dx$

29. Solve: $\frac{dy}{dx} = \frac{1+y^2}{(1+x^2)}$.

30. The probability density function of *X* is given by $f(x) = ke^{-|x|}$,$-\infty < x < \infty$ then find the value of 'k'

PART-III

Note: Answer **any seven** questions. Question No. **40 is compulsory**. **7x3=21**

31. Solve the linear equations $5x - 2y + 16 = 0, x + 3y - 7 = 0$, by Cramer's rule.

32. For any two complex number z_1 and z_2 prove that $|z_1 + z_2| \leq |z_1| + |z_2|$

33. If *k* is real, discuss the nature of the roots of the polynomial equation $2x^2 + kx + k = 0$, in terms of *k*

34. Evaluate : $\int_{-4}^{4} |x + 3|\, dx$

35. Prove that $\left[\vec{a} \times \vec{b}, \vec{b} \times \vec{c}, \vec{c} \times \vec{a}\right] = \left[\vec{a}, \vec{b}, \vec{c}\right]^2$

36. Find the absolute maximum and absolute minimum values of the function $f(x) = 2x^3 + 3x^2 - 12x$ on $[-3,2]$

37. If $u(x, y, z) = xy^2z^3, x = \sin t, y = \cos t, \ z = 1 + e^{2t}$, find $\frac{du}{dt}$.

38. Five fair coins are tossed once and *X* denotes the number of heads. Find the binomial distribution

39. Show that $\neg(p \wedge q) \equiv \neg p \vee \neg q$

40. Solve $\cos(2\sin^{-1}x) = \frac{1}{9}$, if $x > 0$.

PART-IV

Note: Answer **all** the questions. **7x5=35**

41. a) Verify (i) closure property, (ii) commutative property, (iii) associative property, (iv) existence of identity, and (v) existence of inverse for the operation $+_5$on Z_5 using table corresponding to addition modulo 5. **OR**

b) A farmer plans to fence a rectangular pasture adjacent to a river. The pasture must contain $1{,}80{,}000\ sq.mtrs$ in order to provide enough grass for herds. No fencing is needed along the river. What is the length of the minimum needed fencing material?

42. a) If $z = x + iy$ and $\arg\left(\frac{z-i}{z+2}\right) = \frac{\pi}{4}$ show that $x^2 + y^2 + 3x - 3y + 2 = 0$ **OR**

b) Find the area of the region bounded between the parabolas $y^2 = 4x$ and $x^2 = 4y$

43. a) Find the equations of the tangent and normal to ellipse $12x^2 + 9y^2 = 108$ when $\theta = \frac{\pi}{3}$ **OR**

b) Sand is poured at a rate of 50 cubic metre per minute forming a conical pile with a circular base whose half of the height and radius of the base are always equal. How fast is the radius of the pile increasing when the pile is 5 metre radius?

44. a) Solve : $x^4 + 3x^3 - 3x - 1 = 0$ **OR**

b) The rate of increase in the number of bacteria in a certain bacteria culture is proportional to the number present. Given that the number triples in 5 hours, find how many bacteria will be present after 10 hours?

45. a) A rod of length $1.2m$ moves with its ends always touching the coordinate axes. The locus of a point P on the rod, which is $0.3m$ from the end in contact with x -axis is an ellipse. Find the eccentricity.

OR

b) The probability density function of random variable X is given by $f(x) = \begin{cases} k & 1 \le x \le 5 \\ 0 & otherwise \end{cases}$ Find

(i) Distribution function (ii) $P(X < 3)$ (iii) $P(2 < X < 4)$ (iv) $P(3 \le X)$

46. a) Prove by vector method that $\sin(\alpha - \beta) = \sin\alpha\cos\beta - \cos\alpha\sin\beta$

OR

b) Solve $[y(1 - x\tan x) + x^2\cos x]dx - xdy = 0$

47. a) Find the non-parametric form of vector equation, and Cartesian equation of the plane passing through the point (2,3,6) and parallel to the straight lines $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-3}{1}$ and $\frac{x+3}{2} = \frac{y-3}{-5} = \frac{z+1}{-3}$

OR

b) Determine the values of λ for which the following system of equations

$x + y + 3z = 0, 4x + 3y + \lambda z = 0, 2x + y + 2z = 0$ has (i) a unique solution (ii) a non-trivial solution.

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